Inventories and the Role of Goods-Market Frictions for Business Cycles

Wouter J. Den Haan^{*}

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Abstract

Changes in the stock of inventories are important for fluctuations in aggregate output. However, the possibility that firms do not sell all produced goods and inventory accumulation are typically ignored in business cycle models. This paper captures this with a goods-market friction. Using US data, "goods-market efficiency" is shown to be strongly procyclical. By including both a goods-market friction and a standard labor-market search friction, the model developed can substantially magnify and propagate shocks. Despite its simplicity, the model can also replicate key inventory facts. However, when these inventory facts are used to discipline parameter values, then goods-market frictions are quantitatively not very important.

Key Words: Matching models, search frictions, magnification, propagation.

JEL Classification: E12, E24, E32.

^{*}Centre for Macroeconomics, London School of Economics and Political Science, Houghton Street, London WC2A 2AE, UK and CEPR, London, UK. E-mail: wjdenhaan@gmail.com. Financial support from the ESRC grant to the Centre for Macroeconomics is gratefully acknowledged. I also would like to thank Francesco Caselli, Gilles Saint-Paul, Michael McMahon, Thijs van Rens, and Silvana Tenreyro for useful comments.

1 Introduction

Firms are likely to hold back on hiring workers when demand for their products is low and consumers may very well postpone purchases when they worry about becoming unemployed. Such interaction between goods-market and labor-market frictions could deepen economic downturns. In modern business cycle models, such "Keynesian" interaction is typically due to nominal frictions, that is, due to the presence of sticky prices and wages: When prices are sticky, changes in demand have a stronger impact on production and changes in production have a stronger impact on employment when wages are sticky. This paper develops a business cycle model in which such Keynesian interaction is due to the presence of *real* frictions in both the labor market and the goods market. With frictions in both markets, there is a potentially powerful interaction between the goods market and the labor market *even* when prices and wages are flexible. This paper is related to the coordination failure literature, but does not rely on self-fulfilling expectations nor on multiple equilibria.¹

It is common to incorporate labor-market search frictions in business cycle models and this approach is adopted here as well. Recently, several papers have incorporated goods-market search frictions into business cycle models.² Several of these papers assume that prices are flexible and by doing so make clear that Keynesian interaction between goods and labor markets is possible without relying on price rigidities. This paper shares with the recent literature the assumptions that (i) firms face frictions in finding buyers for their products and (ii) the severity of this friction varies over the business cycle. In contrast to the literature, the goods-market friction is not symmetric. The underlying idea is that firms may not sell all their products, for example, because they produce what consumers do not want, but consumers consider what is available and the only cost in acquiring the good is the purchase price. This is a minor difference. But the advantage is that Keynesian results in this paper do not rely on the cyclicality of consumers' effort to acquire goods.³

A more essential aspect in which this paper differs from the literature is that the model includes

¹See Cooper (1999) for an overview of coordination failure models.

²For example, Arsenau (2007), Gourio and Rudanko (2011), Mathä and Pierrard (2011), Petrosky-Nadeau and Wasmer (2011), Bai, Ríos-Rull, and Storesletten (2012), Kaplan and Menzio (2013), and Michaillat and Saez (2013).

³It is not clear whether consumers' effort to acquire goods *relative to* the value of purchases is procyclical or countercyclical. In the models of Petrosky-Nadeau and Wasmer (2011) and Bai, Ríos-Rull, and Storesletten (2012), consumers put in *less* effort trying to acquire goods during recessions, which is bad for firms. In the model of Kaplan and Menzio (2013), unemployed consumers have more time to allocate to activities unrelated to working. Consequently, on average consumers put in *more* effort to acquire goods during recessions, since there are more unemployed during recessions. In the model of Kaplan and Menzio (2013), it is bad for firms if consumers put in more effort, since this means that consumers can visit more stores and bargain for lower prices.

inventories. There are several reasons to include inventories. As documented in this paper, the observed behavior of inventories is very informative about the characteristics of frictions in the goods market and the quantitative importance of such frictions for business cycles. This is not surprising. When there are cyclical changes in the frictions that firms face in selling products, then this is likely to affect the accumulation of inventories. Another important reason to include inventories in business cycle models is that changes in the investment in inventories are a quantitatively important aspect of cyclical changes in GDP. Blinder and Maccini (1991) document that the drop in inventory investment accounted on average for 87 percent of the drop in GNP in the postwar US recessions they considered. This paper confirms the empirical relevance of changes in investment in inventories for cyclical fluctuations in GDP, although the estimates are not as high as the one reported in Blinder and Maccini (1991).

This paper makes four contributions. First, the paper constructs a measure of "goods-market efficiency" and documents its properties. Second, the paper develops a business cycle model with inventories that is characterized by frictions in the labor *and* the goods market. Third, the paper documents that the model can match key aspects of US business cycles and in particular the cyclical behavior of inventories. Fourth, the paper documents the importance of goods market frictions when the model is consistent with the cyclical behavior of inventories. These contributions are discussed in more detail in the remainder of this section.

The measure of goods-market efficiency used is the amount of goods sold relative to the sum of newly produced goods and beginning-of-period inventories. A higher value means that firms sell a higher fraction of available products. This efficiency measure is a simple transformation of the inventory-sales ratio; if the inventory-sales ratio decreases (increases), then the goods-market efficiency measure increases (decreases). Section 2 documents that this measure of goods-market efficiency is strongly procyclical. This is not surprising given that the inventory-sales ratio is known to be countercyclical and the two measures are inversely related.⁴ A novel empirical finding is that the goods-market efficiency measure is negatively related to the beginning-of-period stock of aggregate inventories. This last aspect of goods-market efficiency turns out to play a key role in matching the observed behavior of inventories with the theoretical model.

The empirical findings provide the motivation for the specification of the goods-market friction that firms face in the theoretical model developed. Consistent with the observed positive dependence of goods-market efficiency on aggregate real activity, the paper follows Diamond (1982) and lets

⁴Bils and Kahn (2000) document that the inventory-sales ratio is countercyclical.

goods-market efficiency vary with market size. The idea is that a firm is more likely to find a customer who wants the firm's products in larger markets.⁵ The model incorporates this externality, but the externality is not strong enough to generate multiple equilibria as in Diamond (1982). Additional empirical support for this externality is given in Gavazza (2011); using transactions data for commercial aircraft markets, Gavazza (2011) shows that trading frictions diminish with the thickness of the market. In addition, goods-market efficiency is assumed to decrease when aggregate inventories increase, as indicated by the empirical analysis. Except for the presence of inventories and a goods-market friction, the model is a standard business cycle model with a labor-market search friction.

The model can match key facts regarding the behavior of inventories. Important facts regarding the joint behavior of inventories, sales, and real activity are that sales are *less* volatile than production, investment in inventories is procyclical, and the investment in inventories is positively correlated with sales.⁶ These properties have surprised the profession because they are inconsistent with the view that firms smooth production and use inventories as a buffer against unforeseen sales fluctuations. Building models that can match the facts turned out to be a challenging exercise. There are now several ingenious business cycle models that are consistent with observed behavior, but successful inventory models tend to be characterized by non-trivial features such as Ss bands.⁷ In contrast, the model in this paper is extremely simple and can also match the facts. In existing models, the accumulation of inventories is a non-trivial choice problem for the firm. In the benchmark version of this paper's model, firms always try to sell all available goods and goods end up in inventories only because firms are not successful in selling goods. In this version of the model, firms cannot affect the goods-market friction they face, but they could choose to accumulate additional inventories. However, it is never optimal to do so. In the appendix, a version of the model is developed in which firms can affect the severity of the goods-market friction they face—and thus inventory accumulation—by changing the price they charge. This version is shown to be identical to the simpler version of the model with a slightly adjusted specification for the goods-market friction.⁸

⁵The idea is that sellers offer different types of products and that the chance of producing goods that customers do not want is smaller in bigger markets. That is, as the market grows, the law of large numbers becomes more appropriate and uncertainty about the outcome and the chance of mismatch become smaller.

⁶See Blinder and Maccini (1991), Ramey and West (1999), Bils and Kahn (2000), and McMahon (2011) for a discussion.

⁷Exemplary papers on this road towards success are Eichenbaum (1989), Ramey (1991), Bils and Kahn (2000), Coen-Pirani (2004), and Khan and Thomas (2007).

⁸This modification would be counteracted in the calibration phase, since the calibration procedure matches observed

To match the inventory facts, the behavior of the goods-market efficiency measure has to be consistent with its observed properties. In particular, both the observed positive dependence on aggregate real activity *and* the observed negative dependence of the goods-market efficiency measure on aggregate inventories are necessary. The simplicity of this approach to model inventories makes it possible to incorporate it in a broad range of business cycle models and by doing so include an important factor behind cyclical changes in aggregate output into the analysis.

The model is used to assess the importance of the goods-market friction for magnifying and propagating shocks when prices and wages are flexible. The paper documents that the procyclical aspect of the goods-market efficiency measure can create a powerful mechanism to magnify and propagate shocks. This is not too surprising, since Diamond (1982) shows that multiple equilibria are possible if the dependence of the goods-market friction on aggregate activity is strong enough. A more interesting question is whether cyclical changes in goods-market efficiency are still important when the model is consistent with observed inventory facts. The answer is no for two reasons. The first reason is that the positive dependence of goods-market efficiency on aggregate activity cannot be too strong. Consider a shock that negatively affects real activity. If the goods-market efficiency, i.e., the ease with which firms can find customers, drops a lot during economic downturns, then inventories would increase during recessions, whereas they decrease in the data, and sales would drop by more than output, whereas they drop by less in the data. The second reason is that the negative dependence of the goods-market efficiency measure on aggregate inventories also plays an important role in matching key inventory facts. This negative dependence means that cyclical changes in goods-market efficiency are short-lived. That is, following a negative shock, goods-market efficiency deteriorates initially, but it recovers quickly as the stock of inventories is reduced. The last section of the paper discusses some reasons why cyclical changes in goods-market efficiency may still be important, but the conclusion of this paper is that the observed behavior of inventories suggests that interaction between goods-market frictions and labor-market frictions does not seem to be very important, at least not in the type of model considered here and when prices and wages are flexible.

The remainder of this paper is organized as follows. Section 2 describes the goods-market efficiency measure used, its relationship to the inventory-sales ratio, and describes key aspects of its observed cyclical behavior. Section 3 describes the model. Section 4 motivates the parameter choices. Section 5 discusses the results. The last section concludes.

properties of the total goods-market friction, i.e., the part that firms take as given and the part that firms can control.

2 Empirical motivation

This paper focuses on the role of cyclical fluctuations in the efficiency of the process to get produced products into the hands of buyers. This section documents the cyclical behavior of this "goodsmarket efficiency" and links the results to known properties of the cyclical behavior of inventories.

2.1 Goods-market efficiency

Let Y_t be total production in period t and let X_{t-1} be the stock of inventories carried over from the last period after depreciation. The maximum that could be sold in period t is equal to $Y_t + X_{t-1}$. Actual sales, S_t , are typically less. One reason is that goods that are ready to be sold do not find a buyer in the current period. Another reason is that some finished goods have not ended up on store shelves yet and are not ready to be sold. Finally, sales will also be less than $Y_t + X_{t-1}$ if X_{t-1} includes unfinished goods.

Goods-market efficiency, $\pi_{y,t}$, is defined as

$$\pi_{y,t} = \frac{S_t}{Y_t + X_{t-1}}.$$
 (1)

This measure describes how many goods are sold relative to the sum of newly produced goods and the amount of goods carried over as inventories from last period. The amount produced, Y_t , is equal to the amount sold, S_t , plus the investment in inventories. That is,

$$Y_t = S_t + (X_t^{eop} - X_{t-1}),$$
(2)

where X_t^{eop} is the level of inventories at the end of period t before depreciation. Combining the last two equations gives

$$\pi_{y,t} = \frac{S_t}{S_t + X_t^{\text{eop}}} = \frac{1}{1 + X_t^{\text{eop}}/S_t}.$$
(3)

That is, goods-market efficiency is inversely related to the inventory-sales ratio and both measures can be interpreted as measures that describe the efficiency of getting products in the hands of the customer.⁹

2.2 Cyclical properties of goods-market efficiency

The analysis is based on quarterly private non-farm inventory data from 1967Q1 to 2012Q, published by the Bureau of Economic Analysis.¹⁰ Results reported here are based on *aggregate* data and

⁹If X_{t-1} includes unfinished goods, then the efficiency measure could capture more than just frictions in the goods market. In particular, it could also include efficiencies in the production process.

¹⁰Detailed information about data sources is given in appendix A.

sales data are *final* sales, either final total sales by domestic businesses or final sales of goods and structures. Appendix B.1 reports results based on *disaggregated* data for the following five sectors: durable goods manufacturing, non-durable goods manufacturing, durable goods wholesale, non-durable goods wholesale, and retail.

The data are detrended using the Hodrick-Prescott (HP) filter in order to characterize data properties at business cycle frequencies. Two band-pass filters are used to study the possibility that data properties are different at high frequencies. The first extracts fluctuations associated with cycles that have a period of less than one year and the second those that have a period of less than two years.¹¹

Table 1 provides summary statistics and confirms some well-known facts about inventory behavior. In particular, inventories and sales are positively correlated at business cycle frequencies. At higher frequencies, however, there is a negative correlation between sales and inventories.¹² Sales are also positively correlated with the investment in inventories.¹³ That is, inventories tend to increase during periods when the cyclical component of sales is positive. This property is closely related to another well-known property, namely that output is more volatile than sales.¹⁴ For the series considered here, output is roughly ten percent more volatile. This well-known ordering of volatilities has challenged the literature to come up with innovative inventory theories, since the traditional assumption of increasing marginal costs implies that firms would like to smooth production by using inventories as a buffer to absorb sales shocks.

The mean values of the goods-market efficiency for the two measures are equal to 40% and 55%. That is, quite a large fraction of newly produced output and inventories does not reach consumers within the quarter. Figure 1 displays the cyclical behavior of the goods-market efficiency measure. The solid line corresponds to the cyclical component of GDP (top panel) and the goods-market efficiency based on final sales of goods and structures (bottom panel). To better understand the

¹¹The detrended value of an observation is obtained using a band-pass filter that uses the observation itself and 12 lagging and 12 leading observations.

 $^{^{12}}$ Similar results are reported in Wen (2005).

¹³Since inventory investment can take on negative values, it is not possible to take logarithms to obtain a scalefree variable. The following is done to construct the cyclical component of inventory investment. First, inventory investment is divided by the trend value of GDP. Second, the HP-filter is applied to this ratio.

¹⁴Since output equals sales plus investment in inventories, output is necessarily more volatile than sales if sales and investment in inventories are postively correlated. Here, statistics are calculated for the logarithms of the variables. Consequently, the simple additive relationship no longer holds as an identity, but the logic caries over to the analysis using logarithms.

importance of the cyclical changes, the mean of the goods-market efficiency measure is added to its cyclical component. The figure documents that the efficiency measure is clearly procyclical. Since goods-market efficiency is a monotone inverse function of the inventory-sales ratio, this is just another way to state the well-known fact that the inventory-sales ratio is countercyclical. The correlation between goods-market efficiency and GDP is equal to 0.61 for the measure based on final sales of goods and structures. The magnitudes of the cyclical fluctuations are nontrivial. The cyclical component of the goods-market efficiency varies from a minimum of 38.2% to a maximum of 41.8%. Relative to the inventory-sales ratio, an advantage of the goods-market efficiency measure is that it is easier to interpret the magnitude of its cyclical fluctuations and to understand how important observed cyclical fluctuations potentially are for, for example, firm profitability. In particular, the observed difference between the just reported minimum and maximum values would correspond to a 8.5% drop in the sales price if firms would not be able to sell unsold goods in subsequent periods.¹⁵ If one compares this with, for example, the usual magnitude of fluctuations in aggregate TFP, then these are numbers that cannot be ignored.¹⁶

2.3 Tracking goods-market efficiency over the business cycle

To shed more light on the cyclical properties of goods-market efficiency, the following projection is calculated

$$\widetilde{\pi}_{y,t} = \zeta_y \widetilde{Y}_t + \zeta_x \widetilde{X}_{t-1} + u_t, \tag{4}$$

where the tilde indicates that the series have been detrended. Details of this empirical exercise are given in appendix B.2. For all cases considered, the estimate for ζ_y is positive and the estimate for ζ_x is negative. Moreover, the fit improves considerably if inventories are included in the basis of the projection.

The bottom panel of figure 1 plots the results for the goods-market efficiency measure based on final sales of goods and structures for the preferred detrending procedure. The dotted line indicates the projection of the goods-market efficiency measure on just the cyclical GDP component. The dashed line is the projection on both cyclical GDP and cyclical inventories. The cyclical component of GDP clearly tracks key changes in the goods-market efficiency measures. When inventories are

 $^{^{15}}$ Consequences for firm profits are less dramatic if inventories can be carried into the next period. However, inventory carrying costs are non-trivial. Richardson (1995) argues that inventory carrying costs are between 25% and 55% of the stock of inventories.

¹⁶Recall that the standard deviation of aggregate TFP is typically assumed to be $\sqrt{0.007^2/(1-0.95^2)}$, which is equal to 2.2 per cent.

added to the basis of the projection, the projected values capture the severity of the fall in the goods-market efficiency during downturns much better. This may be surprising, since inventories are procyclical and the projection coefficient for inventories is negative. This would suggest that the fitted value of $\tilde{\pi}_{y,t}$ should decrease by *less* when inventories are added to the projection. The reason this does not always happen is the following. Cyclical fluctuations in inventories are larger than cyclical fluctuations in GDP. Moreover, it takes time to build down the large increase in the cyclical component of inventories that is formed during a boom. Consequently, the cyclical component of inventories can still be positive when the cyclical component of GDP is already negative. During such episodes both the negative cyclical component of GDP and the (still) positive cyclical component of inventories push the value of the goods-market efficiency down. This is exactly what happened during some of the deep recessions in the sample and can explain the improved fit during severe downturns when lagged inventories are included in the projection equation.

The explanatory variables are endogenous variables. Thus, these are just projections and the coefficients do not necessarily capture the causal effect of a right-hand side variable on the dependent variable. Nevertheless, the results do hint at the possibility that the process of getting goods in the hands of the consumer becomes easier when aggregate real activity increases and becomes more difficult (per unit of available good for sale) when firms have more goods in inventories. Independent evidence for the estimates found here is given in section 5 in which it is shown that the theoretical model needs a positive value for ζ_y and a negative value for ζ_x to match observed inventory facts.

2.4 Inventory accumulation during the recent recession

Although, inventories are procyclical at business cycle frequencies, they are countercyclical at higher frequencies as pointed out by Wen (2005) and confirmed here. The latter result is consistent with an increase in inventories at the onset of a recession. However, aggregate inventories follow changes in GDP quite quickly; during the recent recession, aggregate inventories also lag GDP, but the lag seems to be not more than one quarter.¹⁷

The behavior of the aggregate series hide quite divergent behavior for the components. For example, from 2007Q3 to 2008Q2 (2008Q3), inventories of the durables-goods wholesale-trade sector increased by 4.2% (3.2%) compared with a drop in GDP of 1.1% (3.3%). Even larger increases are observed when inventories of particular subsectors are considered. Inventories of the "motor vehicles parts and supplies merchant" wholesale industry increased by 8% (11%) from 2007Q3 to

¹⁷See appendix B.3.

2008Q2 (2008Q3). Interestingly, the inventories of this sector display massive drops in subsequent quarters.¹⁸ Inventories of the computers and software merchant wholesale industry increased by 10% (4%) from 2007Q3 to 2008Q2 (2008Q3). In contrast, these inventories did not display sharp drops in subsequent quarters. The largest increase in inventories is observed in the petroleum and coal product manufacturing industry. Inventories in this sector increased by 23% from 2007Q3 to 2008Q1.

3 Model

There are three types of agents in the economy. The first is a representative household that receives the earnings from its members and determines how much of aggregate income to consume and how much to invest in capital. This representative household consists of a continuum of entrepreneurs and a continuum of workers. This section describes the choice problems of the three different agents, the characteristics of the labor and the goods market, wage setting, and the equilibrium conditions.

Notation and reason for the endowment good. Aggregate variables, such as market prices and choices made by the representative household, are denoted by uppercase characters. Variables associated with choices of the individual firms are denoted by lowercase characters. Prices are expressed in terms of an endowment good. This good plays no role in the model at all, but is helpful to describe price and wage setting. In particular, it makes it clear that the price of the market-produced consumption good is fully flexible and adjusts to clear the goods market. By focusing on the case with flexible prices, it becomes clear that there is an interaction between frictions in the goods market and frictions in the labor market *even* when prices and wages are flexible. All variables that are expressed in units of the endowment good are denoted by a symbol with a circumflex. In appendix B.4, it is shown that the model equations can be rewritten to a system of equations in which the endowment good does not appear.

Household. A representative household chooses the consumption of the market-produced good, C_t , the consumption of the endowment good, $C_{e,t}$, and the amount of capital to carry over into the next period, K_t . For stock variables, such as K_t , the subscript t means that it is determined in period t, and available for production in period t + 1.

¹⁸The American Recovery and Reinvestment Act of 2009 is likely to have played a role, but inventories started to drop before the act was signed into law on February 17 2009.

The household consists of a continuum of workers that supply labor inelastically. The total mass of workers is given by Υ_N and the mass of employed workers is equal to N_t . The representative household receives income from employment, $\widehat{W}_t N_{t-1}$, income from renting out capital, $\widehat{R}_t K_{t-1}$, and income from firm ownership, \widehat{D}_t .

The maximization problem of the representative household is given by

$$\mathbf{V}(\mathbf{S}_{t}) = \max_{C_{t}, C_{e,t}, I_{t}, K_{t}} \frac{C_{t}^{1-\nu} - 1}{1-\nu} + U(C_{e,t}) + \beta \mathbf{E}_{t} \left[\mathbf{V}(\mathbf{S}_{t+1}) \right]$$

s.t.
$$\widehat{P}_{t}C_{t} + \widehat{P}_{t}I_{t} + C_{e,t} = \underline{C}_{e} + \widehat{R}_{t}K_{t-1} + \widehat{W}_{t}N_{t-1} + \widehat{D}_{t},$$
(5)

$$I_t = K_t - (1 - \delta_k) K_{t-1}, (6)$$

where I_t is investment, \underline{C}_e is the quantity of the endowment good received, and S_t is the set of state variables.¹⁹

The first-order conditions are given by

$$\Lambda_{e,t} = \frac{\partial U\left(C_{e,t}\right)}{\partial C_{e,t}},\tag{7}$$

$$\widehat{P}_t \Lambda_{e,t} = C_t^{-\nu},\tag{8}$$

$$\widehat{P}_{t}\Lambda_{e,t} = \beta \mathbf{E}_{t} \left[\Lambda_{e,t+1} \left(\widehat{R}_{t+1} + \widehat{P}_{t+1} \left(1 - \delta_{k} \right) \right) \right].$$
(9)

As explained below, transactions in the goods market are characterized by a friction. However, the friction only affects the ability of the firm to find a trading partner; consumers can buy whatever they want without incurring any disutility or any other type of cost except having to pay for the goods acquired. Consequently, the household problem is characterized by the standard set of equations.²⁰

¹⁹The (not frequently used) symbols for the value function and the set of state variables are in bold and should be distinguished from the symbols for sales, S_t , and vacancies, V_t , which are not bold characters.

 $^{^{20}}$ If the household chooses negative gross investment, then equation (5) implies that capital goods are transformed into goods that are immediately available for consumption without any cost or friction. This is a bit strange, since firms do face frictions when selling goods to consumers. This is not an issue, however, since gross investment turns out to be always positive.

Existing firms/jobs. A firm consists of one entrepreneur and one worker. The firm hires capital to produce output. The Bellman equation of the entrepreneur's problem is given by

$$\widehat{\boldsymbol{v}}(x_{t-1}; \boldsymbol{S}_t) = \max_{y_t, k_t, x_t} \begin{pmatrix} \left(\pi_{y,t} \left(y_t + x_{t-1} \right) \widehat{P}_t - \widehat{R}_t k_t - \widehat{W}_t \right) \\ +\beta \left(1 - \delta_n \right) \operatorname{E}_t \left[\Omega_{t+1} \widehat{\boldsymbol{v}}(x_t; \mathbf{S}_{t+1}) \right] \end{pmatrix}$$
s.t.

$$y_t = \alpha_0 \exp\left(Z_t\right) k_t^{\alpha},\tag{10}$$

$$x_t = (1 - \delta_x) \left(1 - \pi_{y,t} \right) \left(y_t + x_{t-1} \right), \tag{11}$$

where Ω_{t+1} is the marginal rate of substitution between one unit of wealth this period and one unit of wealth the next period. That is,

$$\Omega_{e,t+1} = \frac{\Lambda_{e,t+1}}{\Lambda_{e,t}} = \left(\frac{C_{t+1}}{C_t}\right)^{-\nu} \frac{\widehat{P}_t}{\widehat{P}_{t+1}}.$$
(12)

Moreover, δ_n denotes the probability of exogenous firm exit.²¹ Z_t is an exogenous random variable affecting productivity and its law of motion is given by

$$Z_t = \rho Z_{t-1} + \varepsilon_t \text{ with } \varepsilon_t \sim N(0, \sigma^2).$$

The amount of products available for sale consists of newly produced output, y_t , and inventories available at the beginning of the period t, x_{t-1} . The probability to sell a good is equal to $\pi_{y,t}$. Thus, the quantity of unsold products is equal to $(1 - \pi_{y,t}) (\alpha_0 \exp(Z_t) k_{t-1}^{\alpha} + x_{t-1})$ of which the firm carries a fraction $(1 - \delta_x)$ as inventories into the next period. The parameter δ_x captures both physical depreciation as well as loss in value for other reasons.

Firms take $\pi_{y,t}$ as given. In appendix D, it is shown that this version of the model is identical to a version in which firms can affect the goods-market friction they face by changing the prices they charge when a slightly different specification for the goods-market friction is used.

The following first-order conditions characterize the solution of the entrepreneur's choice problem:

$$\widehat{R}_t = \left(\pi_{y,t}\widehat{P}_t + (1 - \pi_{y,t})\left(1 - \delta_x\right)\widehat{\lambda}_{x,t}\right)\alpha A \exp\left(Z_t\right)k_t^{\alpha - 1},\tag{13}$$

$$\widehat{\lambda}_{x,t} = (1 - \delta_n) \beta \mathbf{E}_t \left[\Omega_{e,t+1} \frac{\partial \widehat{\boldsymbol{v}} \left(x_t; \boldsymbol{S}_{t+1} \right)}{\partial x_t} \right].$$
(14)

Here $\widehat{\lambda}_{x,t}$ is the value of relaxing the constraint given in equation (11). It represents the value of leaving period t with one more unit of inventories (after depreciation). The value of a unit of

 $^{^{21}\}delta_n$ is also the worker separation rate, since each firm consists of one worker.

inventories at the beginning of the period is given by

$$\widehat{\boldsymbol{v}}_{x,t} = \frac{\partial \widehat{\boldsymbol{v}}\left(x_{t-1}; \boldsymbol{S}_t\right)}{\partial x_{t-1}} = \begin{pmatrix} \pi_{y,t} \widehat{P}_t \\ + (1 - \pi_{y,t}) \left(1 - \delta_x\right) \widehat{\lambda}_{x,t} \end{pmatrix}.$$
(15)

Using this equation, first-order condition (14) can be written as

$$\widehat{\lambda}_{x,t} = (1 - \delta_n) \beta \mathbf{E}_t \left[\Omega_{e,t+1} \begin{pmatrix} \pi_{y,t+1} \widehat{P}_{t+1} \\ + (1 - \pi_{y,t+1}) (1 - \delta_x) \widehat{\lambda}_{x,t+1} \end{pmatrix} \right].$$
(16)

Choosing to accumulate additional inventory. In the benchmark version of the model, firms take the goods-market friction as given and passively accumulate inventories. The question arises whether it could be optimal to accumulate *additional* inventories. That is, could it ever be optimal to keep some goods in storage instead of trying to sell them? The answer is no. If a firm puts a unit of goods on the market, then the expected payoff is equal to $\pi_{y,t}\hat{P}_t + (1 - \pi_{y,t})(1 - \delta_x)\hat{\lambda}_{x,t}$. If it chooses to keep the unit in inventories, then the expected payoff is equal to $(1 - \delta_x)\hat{\lambda}_{x,t}$. It would only do the latter if $\hat{\lambda}_{x,t} > \hat{P}_t/(1 - \delta_x)$. Thus, a firm would *choose* to put a good into inventories if the value of doing so is sufficiently above the market value of a market-produced good this period. This never happens.²²

Firm heterogeneity and firm value. A newly created firm starts with zero inventories. As time goes by, the firm will accumulate inventories. Firms only differ in the amount of inventories they hold. Moreover, the only aspect of the distribution of inventories that is relevant for agents' decisions and the behavior of aggregate variables is the *aggregate* level of inventories. Although $\pi_{y,t}$ is allowed to depend on *aggregate* inventories, the assumption is made that $\pi_{y,t}$ does not depend on the *firm's* level of inventories. This assumption implies that $v_{x,t}$ does not depend on the level of x_{t-1} . Consequently,

$$\widehat{\boldsymbol{v}}\left(x_{t-1}; \boldsymbol{S}_{t}\right) = \widehat{\boldsymbol{v}}\left(0; \boldsymbol{S}_{t}\right) + x_{t-1}\widehat{\boldsymbol{v}}_{x,t}.$$
(18)

That is, the value of each firm consists of two parts. The first part is the value of the firm *without* inventories, $\hat{v}(0; S_t)$. The second part is the value of the stock of inventories, $x_{t-1}\hat{v}_{x,t}$. Reallocations

$$\frac{(1-\delta_n)}{\left(\hat{R}_{t+1}/\hat{P}_{t+1}+(1-\delta_k)\right)} \left[\pi_{y,t+1}+(1-\pi_{y,t+1})\left(1-\delta_x\right)\frac{\hat{\lambda}_{x,t+1}}{\hat{P}_{t+1}}\right] = \frac{\hat{\lambda}_{x,t}}{\hat{P}_t} > \frac{1}{1-\delta_x},\tag{17}$$

which implies that $\lambda_{x,t+1}/\hat{P}_{t+1}$ is also bigger than $(1 - \delta_x)^{-1}$ unless the net return on capital $\hat{R}_{K,t+1}/\hat{P}_{t+1} - \delta_K$ is sufficiently negative. Such speculative events do not occur in this model.

²²To understand why this is the case, suppose that there is no uncertainty. If $\hat{\lambda}_{x,t}/\hat{P}_t > (1-\delta_x)^{-1}$, then equations (9) and (16) imply that

of inventories across firms have no aggregate consequences, since $\hat{v}_{x,t}$ does not depend on the level of x_t .

The value of a firm with no inventories is given by

$$\widehat{\boldsymbol{v}}(0;\boldsymbol{S}_{t}) = \begin{pmatrix} \pi_{y,t}\widehat{P}_{t}\alpha_{0}\exp\left(Z_{t}\right)k_{t}^{\alpha}-\widehat{R}_{t}k_{t}-\widehat{W}_{t} \\ +\left(1-\delta_{n}\right)\beta E_{t}\left[\Omega_{t+1}\widehat{\boldsymbol{v}}\left(\left(1-\pi_{y,t}\right)\left(1-\delta_{x}\right)\alpha_{0}\exp\left(Z_{t}\right)k_{t}^{\alpha};\boldsymbol{S}_{t+1}\right)\right] \end{pmatrix}$$

$$= \begin{pmatrix} \pi_{y,t}P_{t}\alpha_{0}\exp\left(Z_{t}\right)k_{t}^{\alpha}-\widehat{R}_{t}k_{t}-\widehat{W}_{t} \\ +\left(1-\delta_{n}\right)\beta E_{t}\left[\Omega_{t+1}\begin{pmatrix} \widehat{\boldsymbol{v}}(0;\boldsymbol{S}_{t+1}) \\ +\left(1-\pi_{y,t}\right)\left(1-\delta_{x}\right)\alpha_{0}\exp\left(Z_{t}\right)k_{t}^{\alpha}\widehat{\boldsymbol{v}}_{x,t+1} \end{pmatrix} \right] \end{pmatrix}.$$
(19)

where k_t is the optimal choice for capital.

Using equation (15), the last equation can be written as

$$\widehat{\boldsymbol{v}}(0;\boldsymbol{S}_{t}) = \left(\begin{array}{c} \left(\begin{array}{c} (\pi_{y,t}\widehat{P}_{t} + (1 - \pi_{y,t})(1 - \delta_{x})\widehat{\lambda}_{x,t})\alpha_{0}\exp\left(Z_{t}\right)k_{t}^{\alpha} \\ -\widehat{R}_{t}k_{t} - \widehat{W}_{t} \end{array} \right) \\ + (1 - \delta_{n})\beta \mathbf{E}_{t}\left[\Omega_{t+1}\widehat{\boldsymbol{v}}(0;\boldsymbol{S}_{t+1})\right] \end{array} \right).$$
(20)

Labor market and labor market friction. Job creation requires an entrepreneur starting a project and finding a worker. The per-period cost of this joint activity is equal to ψ units of the market good. The assumption of free entry implies that in equilibrium the cost of creating a job equals the expected benefit. This means that

$$\psi \widehat{P}_t \Lambda_{e,t} = \pi_{f,t} \beta \mathcal{E}_t \left[\Lambda_{e,t+1} \widehat{\boldsymbol{v}} \left(0; \mathbf{S}_{t+1} \right) \right], \tag{21}$$

where $\pi_{f,t}$ is the number of matches per vacancy.

The total number of jobs created, N_t^{new} , depends on the number of vacancies posted, V_t , and the number of unemployed workers $(\Upsilon_N - N_{t-1})$. The matching technology is characterized by a Cobb-Douglas production function, thus²³

$$N_t = (1 - \delta_n) N_{t-1} + \phi_0 V_t^{\phi_1} (\Upsilon_N - N_{t-1})^{1 - \phi_1}, \text{ and}$$
(22)

$$\pi_{f,t} = \phi_0 \left(\frac{\Upsilon_N - N_{t-1}}{V_t}\right)^{1-\phi_1}.$$
(23)

Total investment in job creation is equal to ψV_t .

²³We allow for the possibility that $N_t^{\text{new}} > V_t$, that is, the number of matches could exceed the number of vacancies. In simulated data this does happen, but not very often. If it happens, then firms end up with more than one worker per vacancy. This is not problematic as long as $\pi_{f,t}$ is not interpreted as a probability. Imposing that $N_t^{\text{new}} \le V_t$ makes it more difficult to solve the model accurately. The case in which $N_t^{\text{new}} > (\Upsilon_N - N_{t-1})$ did not occur.

Goods market and the goods-market friction. In the description above, firms do not always sell their products. This is motivated with a very simple matching friction according to which the firm does not find a buyer for every product it puts up for sale. If the standard approach would be used, then the amount of goods available *as well as* the search effort by consumers would affect total sales. It obviously makes sense to assume that consumers have to put in some effort to buy products, which for some consumers is an enjoyable activity and for some it is not. It is less clear, however, whether *changes* in the amount of effort that consumers put into the activity of acquiring goods are important for cyclical fluctuations in the number of goods firms sell when one controls for changes in demand for the good itself. Such changes do play a role in Petrosky-Nadeau and Wasmer (2011), Bai, Ríos-Rull, and Storesletten (2012), and Michaillat and Saez (2013). In the models of these papers, recessions are deeper because shopping itself requires effort?²⁴ That may be the case, but the search friction adopted here does not rely on changes in the search effort of consumers. Here it is assumed that variations in search effort over and above a minimum level are not important for the actual number of transactions and the following formulation is used:²⁵

$$S_t = \pi_{y,t} \left(N_{t-1} y_t + X_{t-1} \right), \tag{24}$$

and $\pi_{y,t}$ is given by

$$\pi_{y,t} = \underline{\pi}_y + \zeta_y \left(Y_t - \underline{Y} \right) + \zeta_x \left(X_{t-1} - \underline{X} \right), \tag{25}$$

where $\zeta_y \geq 0$, $\zeta_x \leq 0$, and a bar under a symbol indicates that it is the variable's steady state value. A positive dependence of $\pi_{y,t}$ on the size of the market, $Y_t = y_t N_{t-1}$, is similar to the

$$S_{t} = \begin{cases} \pi_{y,t} \left(N_{t-1} y_{t} + X_{t-1} \right)^{\nu_{1}} \underline{E}^{\nu_{2}} & \text{if } E_{t} \ge \underline{E} \\ 0 & \text{if } E_{t} < \underline{E} \end{cases} \quad 0 < \nu_{1}, \nu_{2} \le 1,$$

where E_t denotes the effort level and \underline{E} denotes the minimum effort level, e.g., the cost of going to the shopping mall. If an increase in E_t reduces utility, then $E_t = \underline{E}$. The assumption is made that the disutility of putting in \underline{E} is low enough, so that E_t is always equal to \underline{E} . We also assume that $\nu_1 = 1$. For the results in this paper, the value of ν_1 does not matter, since a process for $\pi_{y,t}$ is chosen such that goods-market efficiency, i.e., the level of sales, S_t , relative to the amount of available goods, $N_{t-1}y_t + X_{t-1}$, mimics the cyclicality of its empirical counterpart. The lower ν_1 , the more procyclical $\pi_{y,t}$ has to be to make goods-market efficiency procyclical, that is, the calibrated value of ζ_y would be higher.

²⁴In fact, one could argue that unemployed workers looking to buy something can devote more time searching for the best "match", which could imply that search frictions in the goods market are *less* severe during recessions, since more consumers are unemployed during recessions.

²⁵This formulation implicitly imposes that customers do put in the minimum level required so that sales are not zero. A more complete specification would be the following:

search externality in the pathbreaking model in Diamond (1982). Moreover, a positive value for ζ_y is consistent with the empirical findings based on aggregate data of section 2.3 and the empirical findings based on commercial aircraft markets of Gavazza (2011). The empirical analysis of this paper indicates a negative dependence of $\pi_{y,t}$ on beginning-of-period aggregate inventories. It does not seem unreasonable, that a higher stock of inventories reduces the chance of selling a given good.²⁶ For example, an increase in inventories could reduce goods-market efficiency if goods are competing for shelve space and/or sales staff. But, this raises the question why it also would not be more difficult to sell goods when the amount of *newly* produced goods, Y_t , increases. However, there is an important difference between a higher GDP, Y_t , and a higher level of aggregate inventories, X_{t-1} . A higher level of GDP not only means that the supply of goods increases, it also means that demand increases, since higher production means higher income. In contrast, a higher level of beginning-of-period aggregate inventories definitely means that the supply of goods is higher, but will in general not lead to an equal increase in income.²⁷

Wages. Instead of relying on a theory such as Nash bargaining to describe wage setting, I adopt a flexible approach to model the behavior of the real wage rate. In particular, the wage rate rule is given by

$$\frac{\widehat{W}_t}{\widehat{P}_t} = \omega_0 \begin{pmatrix} \omega_1 \frac{\left(\left(\pi_{y,t}\widehat{P}_t + (1-\pi_{y,t})(1-\delta_x)\widehat{\lambda}_{x,t}\right)\alpha_0k_t^{\alpha} - \widehat{R}_tk_t\right)}{\widehat{P}_t} \\ + (1-\omega_1) \frac{\left(\left(\pi_y \widehat{P} + (1-\pi_y)(1-\delta_x)\widehat{\lambda}_x\right)\alpha_0\underline{k}^{\alpha} - \widehat{\underline{R}}\underline{k}\right)}{\widehat{P}} \end{pmatrix},$$
(26)

where a lower bar indicates the steady state value, $0 \leq \omega_1 \leq 1$, $0 < \omega_0 < 1$, and all variables are expressed in units of the market-produced good. The two terms on the right-hand side are the level of current-period revenues net of rental costs with unsold goods valued at $(1 - \delta_x)\hat{\lambda}_{x,t}$ and its steady state equivalent. If $\omega_1 = 0$, then the real wage rate is fixed. If $\omega_1 > 0$, then wages increase with the firm's net revenues. ω_0 indicates the average share of revenues net of rental costs that goes to the worker. The other fraction goes to the entrepreneur as compensation for creating the job.

²⁶As shown below, the computational analysis is made a lot easier by letting the goods-market friction that a firm faces depend on *aggregate* inventories and not the firm's own inventory levels. A motivation for the dependence of $\pi_{y,t}$ on *aggregate* inventories is given in appendix D, in which a version of the model is developed in which a firm can affect the goods-market efficiency they face by changing the price it charges.

²⁷Inventories are produced in the past. Workers that produced these inventories were paid in the past. Depending on how inventories are valued, the production of inventories may even have generated income through profits. The actual sale of inventories may generate *additional* income in the current period when the sale price exceeds the accounting price used to value inventories, but the value of this additional income is likely to be less than the total value of the inventories available for sale.

Goods-market equilibrium. Total demand for goods is equal to $C_t + I_t + \psi V_t$. In equilibrium, the price level \hat{P}_t is such that the implied amount that customers demand, S_t , and the implied amount that firms supply, Q_t , is such that

$$S_t = \pi_{y,t} Q_t$$
, where (27)

$$Q_t = N_{t-1}\alpha_0 \exp(Z_t) k_t^{\alpha} + X_{t-1}.$$
 (28)

The easiest interpretation of the goods-market friction is that it literally reduces the amount of goods that can be effectively supplied to customers in the current period. Given the reduction in the supply, this market is identical to a competitive market. $\pi_{y,t}$ can also be interpreted as the probability that a good gets sold. With this interpretation, it is more important to specify what firms are allowed to do during the period. If a firm did not sell some products, then it has an incentive to lower the price of these unsold goods *if* the goods can still be sold within the same period. This possibility would have to be ruled out. That is, firms only find out at the end of the period whether a good is sold or not. At that point, the next period starts. At the beginning of this next period, a good that is newly produced is not distinguishable from a good that was produced in the past and did not sell (adjusted for any possible depreciation). Consequently there is no reason why the firm offering goods out of inventories should charge lower prices.

For either interpretation the question arises whether a firm could not affect the goods-market friction it faces by changing the price they charge. In a standard competitive market, firms would make negative profits if they would charge a price below the market price. Here, existing firms actually make a strictly positive profit, because of the search friction in the labor market. In appendix D, a version of the model is developed in which firms can affect goods-market efficiency and thus inventory accumulation—by changing the price they charge. In equilibrium, the price is such that the benefit of lowering the price, i.e., increasing goods-market efficiency and selling more, is equal to the loss, i.e., having to sell goods at a lower price. This more involved version of the model turns out to be identical to the simpler version discussed here for a slight modification of the specification for $\pi_{y,t}$.

Aggregation and equilibrium. Individual firms have different levels of inventories. For example, newly created firms have no inventories at all. But it is easy to obtain an expression for aggregate inventories. All firms face the same value for $\pi_{y,t}$, which implies that all firms choose the same level for capital, i.e., $k_{i,t} = k_t$. The law of motion for aggregate inventories, X_t , is thus equal

 to

$$\begin{aligned} X_t &= (1 - \delta_n) (1 - \delta_x) \sum_i \left[(1 - \pi_{y,t}) (\alpha_0 \exp(Z_t) k_t^{\alpha}) + x_{i,t-1} \right] \\ &= (1 - \delta_n) (1 - \delta_x) \left[N_{t-1} (1 - \pi_{y,t}) \alpha_0 \exp(Z_t) k_t^{\alpha} \right] + (1 - \pi_{y,t}) X_{t-1} \\ &= (1 - \delta_n) (1 - \delta_x) (1 - \pi_{y,t}) \left(\alpha_0 \exp(Z_t) K_{t-1}^{\alpha} N_{t-1}^{1-\alpha} + X_{t-1} \right). \end{aligned}$$

Equilibrium in the rental market for capital goods requires that

$$N_{t-1}k_t = K_{t-1}, (29)$$

that is, the amount of capital firms choose in period t, k_t , is equal to the available amount of capital per firm. Total amount of cash flows generated in the corporate sector, \hat{D}_t , is given by

$$\widehat{D}_{t} = \pi_{y,t} \widehat{P}_{t} \left(N_{t-1} \alpha_{0} \exp\left(Z_{t}\right) k_{t}^{\alpha} + X_{t-1} \right) - \widehat{W}_{t} N_{t-1} - \widehat{R}_{t} K_{t-1} - \psi V_{t}.$$
(30)

An equilibrium is a set of functions $\pi_y(\mathbf{S}_t)$, $\pi_f(\mathbf{S}_t)$, $\widehat{P}(\mathbf{S}_t)$, and $\widehat{W}(\mathbf{S}_t)$ and a set of policy functions for the agents' choices such that (i) the policy functions solve the corresponding optimization problems taking probabilities and prices as given and (ii) and the policy functions imply $\pi_y(\mathbf{S}_t)$, $\pi_f(\mathbf{S}_t)$, $\widehat{P}(\mathbf{S}_t)$, and $\widehat{W}(\mathbf{S}_t)$.

Walras law. Goods market equilibrium requires that

$$C_t + I_t + \psi V_t = \pi_{y,t} \left(\alpha_0 \exp\left(Z_t\right) K_t^{\alpha} N_t^{1-\alpha} + X_{t-1} \right).$$

This equation is implied by the budget constraint of the household and the definition of \hat{D}_t .

4 Calibration

The parameters β , α , δ_k , and ν are set to standard values. In particular, $\beta = 0.99$, $\alpha = 0.3$, $\delta_k = 0.025$, and $\nu = 1$. Typical values for the parameters of the law of motion for productivity, ρ and σ , are 0.95 and 0.007. In addition, the results are given for a process with a value for ρ equal to 0.7 and a value for σ such that the volatility of Z_t is the same for the two processes. By considering a less persistent process for the stochastic driving variable, it becomes clear that the model can generate very persistent behavior even when Z_t itself is not that persistent. The depreciation rate of inventories, δ_x , is set equal to 0.10. This captures physical depreciation, but also other possible reasons for value reduction and storage costs.²⁸

 $^{^{28}}$ The value of this parameter is conservative. It is slightly lower than the value used by Khan and Thomas (2007), who calculate the cost of inventory storage cost to be equal to 12% of the value of inventories held. Their calculations

The wage process is characterized by two parameters, ω_0 and ω_1 . The value of ω_0 is chosen to match a measure of observed employment volatility, namely $\sigma (\ln N) / \sigma (\ln Y)$. The value of the target is equal to 0.466 which is also used in Den Haan and Kaltenbrunner (2009). Several empirical studies suggest that wages are not that responsive.²⁹ Following Den Haan and Kaltenbrunner (2009), ω_1 is set equal to 3/4, that is, wages respond quite strongly to current-period profits. Thus, the results here do not rely on having sticky wages.³⁰

The specification for goods-market efficiency depends on three parameters, $\underline{\pi}_y$, ζ_y , and ζ_x . The value of $\underline{\pi}_y$ is the steady state value of $\pi_{y,t}$ and is set equal 0.4, which is the average of the observed measure for goods-market efficiency for final sales of domestic businesses, as documented in table 1. As discussed below, the values of ζ_y and ζ_x are chosen to match a measure of the volatility of $\pi_{y,t}$, namely $\sigma(\pi_y) / \sigma(Y)$, and a measure of the volatility of sales, namely $\sigma(S) / \sigma(Y)$.

The remaining parameters are related to employment determination. Following the literature, ϕ_1 is set equal to 0.5, which means that the elasticity of $\pi_{f,t}$ with respect to labor market tightness is equal to one half.³¹ Based on results in Den Haan, Ramey, and Watson (2000), the job destruction rate, δ_n , is set equal to 0.052 and the values for the scaling coefficient in the matching function, ϕ_0 , and the cost of starting a project, ψ , are such that the steady state unemployment rate is equal to 12% and the steady state value for the number of matches per vacancy is equal to 0.71.³² This measure for the unemployment rate takes into account those workers that indicate that they would like to work but are not counted in the formal unemployment definition.

5 Results

Two experiments are discussed to bring to light key properties of the model. In the first experiment, the ability to sell, $\pi_{y,t}$ only depends on aggregate output and not on beginning-of-period aggregate inventories. The parameter affecting the dependence of $\pi_{y,t}$ on aggregate output, ζ_y , is chosen such that the volatility and the procyclical behavior of goods-market efficiency, $\pi_{y,t}$, match their empirical are based on data provided by Stock and Lambert (1987) and Richardson (1995). The estimates of the latter are substantially higher, because they include the cost of money, insurance, and taxes, which should not be part of δ_x in this model.

²⁹This is true for results based on estimated DSGE models and for results based on micro-level wage data. See Barattieri, Basu, and Gottschalk (2010).

³⁰In fact, the value of ω_1 is not important in this paper. The reason is that ω_0 is set to match observed employment volatility. If ω_1 is lowered, then a higher value of ω_0 would ensure that employment volatility would not be affected.

 $^{^{31}}$ Empirical support for this value is given in Petrongolo and Pissarides (2001).

 $^{^{32}}$ The latter is based on van Ours and Ridder (1992).

counterparts. Another key parameter in this experiment is ω_0 , the share of revenues that accrues to the workers. Hagedorn and Manovskii (2008) point out that the response of employment to changes in firm revenues is larger when ω_0 is higher and the profit margin is, thus, lower. Therefore, changes in $\pi_{y,t}$ will have a larger impact on the economy if ω_0 is closer to 1. To discipline the model's response to changes in $\pi_{y,t}$, the value of ω_0 is chosen such that the model generates a realistic amount of employment volatility.³³

In the second experiment, $\pi_{y,t}$ depends on aggregate activity, and—motivated by this paper's empirical findings—depends negatively on the beginning-of-period aggregate level of inventories.

Finding the parameter values at which the model exactly hits the targets entails a non-trivial search in the parameter space. Moreover, the calibration procedure relies on second-order moments, the calculation of which requires a numerical solution of the policy functions. Consequently, a fast solution method is needed. The results reported are based on first-order perturbation. At the calibrated parameter values, the model is also solved with a global solution method and the results reported are very similar for the two solution methods.

5.1 The role of a procyclical goods-market friction for business cycles

As documented in section 2, goods-market efficiency, $\pi_{y,t}$, is procyclical and quite volatile. The ability to sell, $\pi_{y,t}$, affects firm profitability and, thus, aggregate activity and it is in turn affected by the level of aggregate activity. Consequently, variation in $\pi_{y,t}$ could be an important channel through which shocks are magnified and propagated. In this subsection, the specification for $\pi_{y,t}$ is given by

$$\pi_{y,t} = \underline{\pi}_y + \zeta_y \left(Y_t - \underline{Y} \right). \tag{31}$$

That is, $\pi_{y,t}$ is allowed to depend on aggregate real activity, but not on aggregate inventories. Model properties are presented in table 2, which reports unconditional business cycle moments, and in figure 2, which displays the impulse response functions (IRFs).

The role of inventories for GDP fluctuations. First consider the benchmark results when ζ_y and ω_0 are chosen such that the model exactly matches the observed cyclical behavior of goods market efficiency and employment. Since goods-market efficiency is a simple transformation of

³³It is not straightforward to calibrate ω_0 using direct measures of entrepreneurial compensation. Observed profit shares include compensation for equity financing, while in the model $1 - \omega_0$ is only the compensation for the entrepreneurial activity of creating a job.

the inventory-sales ratio, the calibration automatically ensures that the model also matches the cyclical behavior of the inventory-sales ratio. Table 2 documents that the model predicts the typical ordering of the volatility of consumption, investment, and output. The calculated shares of investment in inventories for GDP fluctuations are equal to 0.149 and 0.094 when ρ is equal to 0.7 and 0.95, respectively.³⁴ The empirical counterpart is equal to 0.193. Thus, a non-trivial part of GDP fluctuations is attributable to investment in inventories, although this version of the model somewhat underpredicts the importance of inventories for business cycle fluctuations of GDP.

At the calibrated parameter values, the IRFs of inventories and sales associated with a positive shock to Z_t are positive at all time horizons. With both responses being positive, it is not surprising that the model correctly predicts that inventories are positively correlated at business cycle frequencies. The model also correctly predicts that inventories and sales are *negatively* correlated at higher frequencies. This is more surprising given that the IRFs of both variables are positive. The reason is that the response of inventories is a bit delayed. This means that the high-frequency component of the inventories response is initially negative, whereas the high-frequency component of the real activity response is initially positive.

Magnification and persistence. The autocorrelation coefficients for employment and output indicate that the model is capable of adding quite a bit of persistence. For example, when $\rho = 0.7$, the autocorrelation coefficients are equal to 0.982 and 0.997 for employment and output, respectively.³⁵

Figure 2 displays the IRFs of employment, output, and goods-market efficiency. To facilitate comparison, the IRF of productivity is also shown in the panels for the employment IRF and the output IRF. The variance of the innovation is chosen such that the unconditional variance of Z_t is the same for the two values of ρ . Consequently, the process with the higher value for ρ has a smaller innovation variance and, thus, smaller initial responses. The IRFs are given for three different values of ζ_y . The first value is the one for which model predictions for $\pi_{y,t}$ match the observed cyclical behavior of its empirical counterpart. The second value of ζ_y considered is 0. A

³⁴Following Fujita and Ramey (2009), this contribution is calculated as follows. Here, \tilde{Y}_t is the cyclical component of GDP divided by its trend value, \tilde{X}_t is the cyclical component of investment in inventories divided by the trend value of GDP, and \tilde{Y}^* is defined by $\tilde{Y}_t = \tilde{Y}^* + \tilde{X}_t$. The latter identity implies that $\operatorname{variance}(\tilde{Y}_t) = \operatorname{covariance}(\tilde{Y}_t, \tilde{Y}_t^*) + \operatorname{covariance}(\tilde{Y}_t, \tilde{X}_t)$. The fraction of GDP fluctuations that is attributed to investment in inventories is, thus, given by $\operatorname{covariance}(\tilde{Y}_t, \tilde{X}_t)$ /variance (\tilde{Y}_t) .

³⁵Since filtering also affects the autocorrelation, the unfiltered series are used to calculate these statistics.

comparison of the responses when $\zeta_y = 0$ with the responses for the calibrated value of ζ_y reveals the role of goods-market friction in magnifying and propagating shocks. The third value of ζ_y is such that the model responses to the *non-permanent* shock considered here are close to being permanent. By considering higher values of ζ_y one learns what the role of goods-market frictions can be if parameter choice is not constrained by the observed volatility of $\pi_{y,t}$.

The graphs show that the goods-market friction magnifies the employment and output responses to a shock to Z_t . This is not surprising. A negative shock to Z_t reduces the size of the market, which increases the severity of the goods-market friction, which in turn reduces profits and, thus, vacancies, and employment, that is, a further reduction in the size of the market. The graph also shows that the employment and output responses are substantially more persistent than the responses of Z_t itself. This is also true when $\zeta_y = 0$ and $\pi_{y,t}$ is, thus, constant. When ζ_y equals zero, shocks are propagated because of the matching friction and the desire to smooth consumption. The responses are more persistent, however, when ζ_y is equal to its calibrated value and substantially so when $\rho = 0.7$. The reason for the additional persistence is the following. If the goods-market friction is more severe, then expected firm profits are lower. Consequently, firms post less vacancies. Lower vacancies imply a lower job-finding rate, which directly implies a more persistent law of motion for employment.

When $\rho = 0.95$, that is, when the underlying shock is already quite persistent, then the model does not add a lot of magnification and additional persistence when ζ_y is equal to its calibrated value. When ζ_y is increased above its calibrated value, however, then the goods-market friction also generates remarkable propagation when $\rho = 0.95$.

Why this version cannot match all inventory and sales facts. At the calibrated parameter values, the model predicts that output and sales have roughly the same volatility. In the data, however, sales are *less* volatile than output. This somewhat surprising empirical finding has triggered an extensive literature with ingenious attempts to build models to get this right. The model developed here could generate the right ordering for the volatility of sales and output quite easily. As indicated in the " $\zeta_y = 0$ " column in table 2, sales are substantially less volatile than output when goods-market efficiency is constant, especially when $\rho = 0.7$. When $\pi_{y,t}$ is constant, then sales are simply a fraction of the amount of available goods for sale, that is, newly produced goods *plus* the stock of inventories. The latter is a stock variable and less volatile than output. Consequently, when sales are a constant fraction of the sum of output and inventories, then sales will be less volatile

than output.

The problem with setting ζ_y equal to zero and keeping $\pi_{y,t}$ constant, however, is that the model would no longer generate the right cyclical behavior for the goods-market efficiency measure, $\pi_{y,t}$, and, thus, would not generate the right cyclical behavior of the inventory-sales ratio. Starting at zero, an increase in ζ_y induces volatility in the goods-market efficiency measure, which is consistent with the data. As long as ζ_y is low enough, the model also correctly predicts that sales are less volatile than output. However, when ζ_y is such that the model matches the volatility of $\pi_{y,t}$, the volatility of sales exceeds the volatility of output. Consequently, the model cannot match both the correct procyclical behavior of $\pi_{y,t}$ and the right relative volatility of sales and output by only changing ζ_y . In the next subsection, it will be shown that the model can match both properties by allowing $\pi_{y,t}$ to also depend on aggregate inventories.

The role of the goods-market friction when $\zeta_x = 0$. The finding that the model's implications become increasingly at odds with well-known facts from the inventory literature as ζ_y takes on higher values also means that the role of the goods-market friction for magnification and propagation is limited. This is most clear when $\rho = 0.95$. In this case, the value of ζ_y , which directly affects the magnitude of cyclical fluctuations in the goods-market friction, can be increased a lot before the model's solution becomes explosive. As documented in figure 2, the model generates stunning magnification and propagation at high values for ζ_y . Moreover, figure 2 also documents that $\pi_{y,t}$ drops just a few percentage points at the highest value for ζ_y considered. Although the implied volatility for $\pi_{y,t}$ is higher than what is observed in the data, the generated changes in $\pi_{y,t}$ do not seem outlandish. However, some implications for the model's properties regarding inventories are clearly inconsistent with the data when ζ_y takes on high values.

It is quite intuitive that making goods-market frictions more important will at some point imply that the model's predictions for sales and inventories deteriorates. Consider a negative TFP shock. The reduction in economic activity induces a reduction in $\pi_{y,t}$. The larger the value of ζ_y , the larger the reduction in $\pi_{y,t}$, which in turn implies stronger magnification and more persistence. But the reduction in $\pi_{y,t}$ also implies that less is sold relative to what is produced. As the reduction in $\pi_{y,t}$ becomes larger, then at some point sales will drop by *more* than output and inventories will *increase*. Both properties are inconsistent with observed facts. Again, consider the case when $\rho = 0.95$ and ζ_y is set equal to its highest possible value. In this case, the standard deviation of sales is 1.823 times the standard deviation of output, whereas the empirical ratio is only 0.901. Similarly, the correlation between inventories and sales is *negative* whereas it is positive in the data.

5.2 Results when goods market friction also depends on inventories

The results discussed so far show that the model cannot simultaneously match the correct cyclical behavior of goods-market efficiency and predict that sales are less volatile than output when $\pi_{y,t}$ only varies with aggregate output. The empirical results in section 2 indicate, however, that $\pi_{y,t}$ not only depends on output, but also depends (negatively) on beginning-of-period aggregate inventories. To capture both aspects the following specification for $\pi_{y,t}$ is considered:

$$\pi_{y,t} = \underline{\pi}_y + \zeta_y \left(Y_t - \underline{Y} \right) + \zeta_x \left(X_{t-1} - \underline{X} \right) \text{ with } \zeta_y > 0, \, \zeta_x < 0.$$
(32)

The values of ζ_y , ζ_x , and ω_0 are chosen to match the observed volatility of employment, the observed cyclical behavior of $\pi_{y,t}$, and the observed value for the volatility of sales relative to the volatility of output. Table 3 reports unconditional business cycle moments and figure 3 displays the impulse response functions (IRFs).

The role of inventories for GDP fluctuations. As documented in table 3, this version of the model also generates the right ordering for the volatility of consumption, investment, and output. At the calibrated parameter values, the share of investment in inventories for cyclical fluctuations in GDP is equal to 0.240 when ρ equals 0.7 and 0.259 when $\rho = 0.95$. Both are fairly close to the observed share which is equal to 0.193. Moreover, at the calibrated parameter values the model predicts correctly (again) that inventories and sales are positively correlated at business cycle frequencies and negatively correlated at high frequencies.

Why this version can match the inventory and sales facts. As pointed out in the previous subsection, $\pi_{y,t}$ cannot respond too strongly to changes in real activity, because sales would be more volatile than output if the response is large enough. On the other hand, the response has to be sufficiently strong to ensure that $\pi_{y,t}$ is sufficiently volatile. The dilemma of matching both properties can be solved by letting $\pi_{y,t}$ depend positively on real activity (that is, $\zeta_y > 0$) and as indicated by the empirical findings discussed in section 2—negatively on beginning-of-period aggregate inventories (that is, $\zeta_x < 0$). In fact, with the appropriate choice of ζ_y and ζ_x the model can exactly match the observed volatility and procyclical behavior of $\pi_{y,t}$ (and, thus, match the observed cyclical behavior of the inventory-sales ratio) as well as exactly match the observed volatility of sales relative to the volatility of output. Additional support for the specification used can be found in the fact that the calibrated values for ζ_y and ζ_x are not that different from the empirical estimates discussed in section 2. For example, when $\rho = 0.95$, then the calibrated values are 0.161 and -0.191 for ζ_y and ζ_x , respectively. The empirical estimates for these two parameters are equal to 0.25 and -0.14.³⁶

What does the calibrated specification for $\pi_{y,t}$ imply for the behavior of $\pi_{y,t}$ following a shock to Z_t . The results are given in the two panels of the bottom row of figure 3. Similar to the results with $\zeta_x = 0$, $\pi_{y,t}$ displays a sharp drop when Z_t is hit by a negative shock. In contrast to the results with $\zeta_x = 0$, $\pi_{y,t}$ recovers rapidly and goes *above* its pre-shock value as the reduction in aggregate inventories puts upward pressure on $\pi_{y,t}$. The result that the response of $\pi_{y,t}$ switches signs makes it possible to have a sufficiently volatile $\pi_{y,t}$ without making sales too volatile.

The role of the goods-market friction when $\zeta_x < 0$. Compared with other models in the literature that incorporate inventories into business cycle models, the model developed here is remarkably simple. Despite its simplicity, it can generate key facts about inventories and it captures the observed importance of investment in inventories for fluctuations in aggregate output. The question arises whether goods-market frictions are an important channel through which shocks get magnified and propagated when the model matches all key facts regarding the joint behavior of inventories, sales, and output.

Figure 3 plots the employment and output IRFs at the calibrated values for ζ_y and ζ_x and when ζ_y is set as high as possible without having explosive responses, keeping ζ_x fixed. Resembling the results in section 5.1, employment and output responses are larger and more persistent at higher values of ζ_y . Thus, by increasing ζ_y the model can magnify and propagate shocks, but an increase in ζ_y above its calibrated value comes at the cost of doing worse in terms of matching the observed behavior of inventories. In particular, sales become too volatile relative to output.

The question arises how the model in which $\pi_{y,t}$ is constant compares to the model in which $\pi_{y,t}$ responds to real activity and accumulated inventories as indicated by the calibrated values for ζ_y and ζ_x . That is, how important are changes in goods-market efficiency when the model is calibrated to be consistent with the joint behavior of inventories, sales, and output. The IRFs for the case when both ζ_y and ζ_x are equal to zero are also plotted in figure 3. The figure shows that eliminating the calibrated fluctuations in $\pi_{y,t}$ results in *more* magnification and *more* persistence, whereas the

³⁶Since the regression is affected by endogeneity issues, the estimates of ζ_y and ζ_x should be interpreted with care, but these theoretical results suggest that a more causal interpreted may not be that unreasonable.

opposite was found in the previous subsection. The reason is the following. Consistent with the results in the previous subsection, eliminating the positive dependence of $\pi_{y,t}$ on real activity leads to less magnification and less persistence. Eliminating the negative dependence of $\pi_{y,t}$ on aggregate inventories, however, leads to more magnification and more persistence and this effect turns out to be stronger. The latter effect is only slightly stronger and the employment and output IRFs based on the calibrated specification for $\pi_{y,t}$ are quite similar to the IRFs based on a constant value for $\pi_{y,t}$. Although the richer specification for $\pi_{y,t}$ makes it possible to match the key facts regarding the behavior of inventories, sales, and output, it also means that variation in the goods-market friction no longer works as a mechanism to magnify and propagate shocks. The concluding section points out that this does not necessarily mean that goods-market frictions do not play an important role in the transmission of shocks, but this role does seem to be restricted by the observed behavior of inventories. At least in this type of model without any other type of friction such as sticky prices.

6 Goods-market frictions, the verdict

The presumption that frictions in goods markets and frictions in labor markets, and especially their interaction, are important for business cycles seems reasonable. If frictions prevent goods market from working efficiently, then this is likely to affect firms' sales and firms' hiring decisions. Similarly, if labor markets do not work efficiently, then this will affect the job-finding rate, which in turn will affect goods-market activity. This paper formalizes this idea and shows that a model with goods and labor-market frictions can quite easily magnify and propagate shocks. Moreover, the model can also replicate key aspects of the behavior of inventories, sales, and output. The problem is that it cannot do both at the same time. Does this mean that realistic goods-market frictions do not change the dynamics of business cycles very much and that there is, thus, not much point in incorporating a goods-market friction in business cycle models?

Before addressing these questions, the key aspects of the restrictions that observed inventories, sales, and output data impose on cyclical changes in the goods-market friction are highlighted. Suppose that a negative shock hits the economy. If goods-market frictions are procyclical, then this would mean that such a negative shock would impede sales. The data imply, however, that firms manage to let output drop by *more* than sales. This *seems* to indicate that firms are quite efficient in scaling down the size of operations during downturns. Moreover, if output drops by more than sales, then the probability to sell, i.e., the severity of the goods-market friction, cannot have

worsened too much. That is, the level of sales are not that bad *relative to* the level of output. If the goods-market friction would worsen too much, then a negative shock would lead to an *increase* in inventories and the drop in sales would *exceed* the drop in output.

Nevertheless, it is still a good idea to incorporate goods-market frictions, since—as documented in this paper—a simple goods-market friction can match key facts about inventories. Given that changes in the investment in inventories are known to be important for GDP fluctuations, it makes sense to include inventories in business cycle models.

Now consider the question whether the results in this paper indicate that cyclical changes in goods-market frictions are unlikely to be quantitatively important for aggregate fluctuations. The provision of many types of services does not allow for inventories. If a hairdresser has no customers, then this does not lead to an increase in inventories. If there are no inventories, then the observed behavior of inventories cannot impose restrictions on the properties of the goods-market friction like they do in this paper. But the question arises whether the behavior of goods-market frictions would be very different for services than for manufacturing and wholesale.

Another reason why goods market frictions could be more important than the results in this paper indicate is that the cyclicality of the goods-market friction measure used in this paper understates the procyclical behavior of the true goods-market friction, because this paper's measure is based on *actual* output instead of *potential* output. To explore this possibility, consider the following example. During normal times, firms produce 100 goods, start the period with 100 goods in inventories, and sell 100 goods. Thus, the sell probability is equal to one-half. In addition, suppose that firms would like to reduce output to 80 goods when the economy is hit by a negative shock and the sell probability would remain equal to one-half. If the sell probability would indeed remain constant, then sales would drop by 10 to 90, which is less than the drop in output, and inventories would drop to 90. Both responses are consistent with the data. Now suppose that the sell probability does not remain equal to one-half, but drops to one third during an economic downturn. If the firms would still produce 80, then sales would drop to 60, i.e., one third of 180 (80 produced goods and 100 from inventories). Inventories would increase and the drop in sales is bigger than the drop in output. Both responses are inconsistent with the data, which is the reasons why the calibrated models did not consider such large changes in the goods-market friction. But now suppose that firms can choose to keep labor idle and that there is some benefit of doing so.³⁷ Faced with a sharp drop in sales, one could argue that the firm should lower output further, say to 20 units and enter

³⁷The benefit could be a reduction in material costs or a direct utility benefit of working less.

the market this period with 20 newly produced goods and 100 goods in inventories. If the firm still sells 60, then the *observed* value for the sell probability would be equal to one-half, that is, the observed goods-market friction would show no change even though the firm faces a sharp reduction in the sell probability if one considers actual sales relative to what the firm could produce given the size of its workforce.

Unfortunately, there are several problems with this reasoning. First, in this numerical example the amount firms can sell does not depend on the amount of goods that are available. That is, sales are kept constant at 60 when production is reduced. But the idea of the goods-market friction is that mismatch between what producers produce and what consumers want is smaller when markets are bigger. More importantly, if firms can lower actual production during recessions without negatively affecting the amount they sell, then the question arises why they would not do so during normal times? If output can be reduced without negatively affecting sales, then firms could lower production during normal times as well, for example, to a level of 50 units, which—if sales remain fixed at 100—would imply that the probability to sell increases from one-half to two-thirds. One would have to argue that this increase in efficiency only happens during downturns, perhaps because operating efficiently is only essential during downturns or the chance of stockouts are less problematic during downturns.

Finally, consider the possibility that inventories do not increase during economic downturns and the sell probability does not drop by that much exactly because the supply of goods falls sharply during down turns. This may very well be the case, but if—in the end—the sell probability does not drop by that much, then why would output drop by so much? If the entrepreneur's share of the surplus, $1 - \omega_0$, is small on average, then small changes in $\pi_{y,t}$ can induce large proportional changes in the entrepreneur's revenue, which in turn leads to large fluctuations in job creation and aggregate output. To generate sufficiently volatile employment and aggregate output, this paper follows Hagedorn and Manovskii (2008) and adopts values for ω_0 that are already quite high.³⁸ But choosing an even higher value for ω_0 would not change the conclusion. For example, consider the case when ρ is equal to 0.95, $\zeta_y = 0.161$, and $\zeta_x = 0$. As documented in figure 2 and table 2, in this case the goods-market friction magnifies shocks somewhat, but not by much. If ω_0 is increased with one percentage point, then shocks have a substantially larger impact on the economy. For example, the maximum drop in employment increases considerably, namely from 4.8% to 7.0%. But a similar increase is observed for the responses when $\zeta_y = 0$. And relative to the " $\zeta_y = 0$ " responses, the

 $^{^{38}\}mathrm{See}$ tables 2 and 3.

proportional increase in responses when ζ_y is increased to 0.161 is very similar for the two values of ω_0 considered.

A Data sources

The analysis is based on quarterly data from 1967Q1 to 2012Q1. Data are from the NIPA tables of the Bureau of Economic Analysis (BEA). All data are measured in chained 2005 dollar and are seasonally adjusted. Gross Domestic Product (GDP) is taken from table 1.1.6. The GDP data were last revised on June 28 2012.

The data based on final sales uses as inputs: nonfarm inventories to final sales, nonfarm inventories to final sales of goods and structures, and nonfarm inventories. Sales data and the goods-market efficiency measure are constructed using these series. Data are from table 5.7.6A (data up to 1997) and table 5.7.6B (data from 1997 onward). The data up to 1997 are based on the Standard Industrial Classification (SIC) and the data from 1997 are based on the North American Industry Classification System (NAICS). The change in classification system has no effect on these aggregate series. The data from table 5.7.6A were last revised August 11 2011. The data from table 5.7.6B were last revised June 28 2012.

The disaggregated sector data uses as inputs: end-of-period manufacturing and trade inventories and manufacturing and trade sales. The inventory-sales ratio and the goods-market efficiency are constructed using these series. The inventory data are from table 1AU2 (data up to 1997 based on SIC) and table 1BU (data from 1997 onward based on NAICS). The overlapping data in 1997 are used to rescale the data series and eliminate the discontinuity. The sales data are from table 2AU (data up to 1996 based on SIC) and table 2BU (data from 1997 onward based on NAICS). No overlapping data are available. Therefore, hypothetical 1997Q1 SIC-based observations are obtained by extrapolation. The hypothetical 1997Q1 SIC-based observations and the actual 1997Q1 NAICS observations are used to rescaled the series and eliminate the discontinuity. The results presented here are based on the case when the growth rates from 1996Q3 to 1996Q4 is used to construct the hypothetical 1997Q1 observations. Alternatives based on growth rates from the 1996Q1-1998Q4 period give very similar results. The data from tables 1AU2, 2AU, 1BU, and 2BU were last revised August 11 2011, August 5 2009, June 1 2012, and June 1 2012, respectively.

B Additional results

B.1 Results for dissagregated data

This appendix reports results based on *disaggregated* data for the following five sectors: durable goods manufacturing, non-durable goods manufacturing, durable goods wholesale, non-durable goods wholesale, and retail.

Using the series based on gross sales, the mean efficiency measures are substantially higher and vary between 62% for wholesale durables and 79% for wholesale non-durables. Sales data for the disaggregated series are *gross* series, whereas the results reported in the main text are based on final sales. Consequently, the results for sectoral series possibly provide an inflated view of the efficiency of the sector as a whole, since gross sales include sales to other firms within the same sector.

Table 4 documents that the results are similar to those presented in the main text for several of the series based on sectoral gross sales, but not for all. In particular, the goods-market efficiency measures are procyclical for the durable and non-durable goods manufacturing sector, for the durable goods wholesale sector, but they are acyclical for the non-durable wholesale sector and the retail sector. The question arises whether the comovement between real activity and the goods-market efficiency in these two sectors remains low if a real activity measure for the sector itself would be used instead of GDP. One can construct production measures that are consistent with the sales and inventory data by using the following equation:³⁹

$$Y_t = S_t + \left(\frac{X_t}{1 - \delta_x} - X_{t-1}\right). \tag{33}$$

Using this real activity measure instead of GDP, the correlation coefficients for the non-durable goods wholesale and the retail sector, are substantially higher, namely 36% and 35%, respectively. This is still lower, however, than the corresponding numbers for the other sectors.

Section 2 in the main text documents that the correlation between GDP and goods-market efficiency is negative at high frequencies. For the series based on the gross sales measures, the correlation clearly drops if the frequency considered increases, but only four of the ten correlation coefficients turn negative.

For the measures based on gross sales, the volatility of sectoral output is always higher than the volatility of sectoral sales, but the differences are smaller than those reported in the main text that are based on final sales.

³⁹For these calculations, the depreciation of inventories, δ_x , is set equal to ten percent, but the results are robust to changes in the depreciation rate used.

B.2 Results for the projection exercise

In this appendix, the results of the following projection are discussed:

$$\widetilde{\pi}_{y,t} = \zeta_y \widetilde{Y}_t + \zeta_x \widetilde{X}_{t-1} + u_t, \tag{34}$$

where the tilde indicates that the series have been detrended. For this exercise, detrending with a third-order deterministic trend is considered in addition to the HP filter.⁴⁰ Table 5 documents that the estimates for ζ_y are positive and those for ζ_x are negative.⁴¹ Figures 4 and 5 plot goods-market efficiency measures, together with projected values, when data are detrended using the HP filter and a deterministic trend, respectively. The dotted lines are the projection of the goods-market efficiency measure on just the cyclical GDP component. The dashed line is the projection on both cyclical GDP and cyclical inventories. The cyclical component of GDP clearly tracks key changes in the goods-market efficiency measures. As documented by these figures and the R-squares of table 5, the fit improves substantially if the cyclical component of inventories is included in the basis of the projection. Regarding the magnitudes, the largest coefficients for ζ_y are found for the durable goods manufacturing sector for which a 1% increase in the cyclical component of GDP corresponds to a 0.60 percentage point increase in the goods-market efficiency. The smallest effect is found for the non-durable wholesale sector for which the coefficient is only 0.06.

B.3 Aggregate inventories

Figure 6 plots the cyclical components of GDP and non-farm aggregate inventories. The figure clearly shows the positive correlation of inventories and GDP, but the figure also documents that the cyclical component of inventories lags output and frequently continues to decrease (increase) when the cyclical component of GDP has already passed its turning point and is increasing (decreasing). Even during deep recessions, the drop in output is followed by a rapid decline in inventories.

⁴⁰This is not only done to document robustness. Although the exercise is interpreted as a projection and not a regression, it still would be nice if the right-hand side variables are less endogenous. The problem with the HP-filter is that the right-hand side variables would not even be predetermined.

⁴¹Table 1 in the main text and table 1 in this appendix document that the same is true for the unconditional correlation of $\pi_{y,t}$ and the two right-hand side variables.

C Simplified model equations

In the model developed in section 3 of the main text, the price level of the market-produced consumption good, \hat{P}_t , is allowed to vary freely. That is, the model does not rely on sticky prices. As long as the specification for wages is for real wages, then the model can be represented by a set of equations in which the price of the market-produced consumption good is the numeraire and equal to 1 and the endowment good does not appear. This latter system is simpler, but when the price of the market-produced consumption good is the numeraire are allowed to vary with market conditions.

This simplified model is given by the following set of equations:

$$C_{t} + I_{t} + \psi V_{t} = \pi_{y,t} \left(\alpha_{0} \exp\left(Z_{t}\right) K_{t}^{\alpha} N_{t}^{1-\alpha} + X_{t-1} \right),$$
(35)

$$I_t = K_t - (1 - \delta_k) K_{t-1},$$
(36)

$$\Lambda_t = C_t^{-\nu},\tag{37}$$

$$\Lambda_t = \beta \mathcal{E}_t \left[\Lambda_{t+1} \left(R_{t+1} + (1 - \delta_k) \right) \right], \tag{38}$$

$$\Omega_{t+1} = \frac{\Lambda_{t+1}}{\Lambda_t} = \left(\frac{C_{t+1}}{C_t}\right)^{-\nu},\tag{39}$$

$$R_{t} = (\pi_{y,t} + (1 - \pi_{y,t}) (1 - \delta_{x}) \lambda_{x,t}) \alpha A \exp(Z_{t}) k_{t}^{\alpha - 1},$$
(40)

$$\lambda_{x,t} = (1 - \delta_n) \beta \mathbf{E}_t \left[\Omega_{t+1} \left(\begin{array}{c} \pi_{y,t+1} \\ + (1 - \pi_{y,t+1}) (1 - \delta_x) \lambda_{x,t+1} \end{array} \right) \right], \tag{41}$$

$$\boldsymbol{v}(0;\boldsymbol{S}_{t}) = \left(\begin{array}{c} \left(\begin{array}{c} \pi_{y,t} + (1 - \pi_{y,t}) \left(1 - \delta_{x}\right) \lambda_{x,t} \right) \alpha_{0} \exp\left(Z_{t}\right) k_{t}^{\alpha} \\ -R_{t}k_{t} - W_{t} \end{array} \right) \\ + \left(1 - \delta_{n}\right) \beta \mathbf{E}_{t} \left[\Omega_{t+1} \boldsymbol{v}(0;\boldsymbol{S}_{t+1})\right] \end{array} \right),$$
(42)

$$\psi = \pi_{f,t} \beta \mathbf{E}_t \left[\Omega_{t+1} \boldsymbol{v} \left(0; \mathbf{S}_{t+1} \right) \right], \tag{43}$$

$$N_t^{\text{new}} = \phi_0 V_t^{\phi_1} \left(\Upsilon_N - N_{t-1} \right)^{1-\phi_1}, \qquad (44)$$

$$N_t = (1 - \delta_n) N_{t-1} + N_t^{\text{new}},$$
(45)

$$\pi_{f,t} = \phi_0 \left(\frac{\Upsilon_N - N_{t-1}}{V_t}\right)^{1-\phi_1},\tag{46}$$

$$\pi_{y,t} = \underline{\pi}_y + \zeta_y \left(Y_t - \underline{Y} \right) + \zeta_x \left(X_{t-1} - \underline{X} \right), \tag{47}$$

$$X_{t} = (1 - \delta_{n}) (1 - \pi_{y,t}) (1 - \delta_{x}) \left((\alpha_{0} \exp(Z_{t}) K_{t-1}^{\alpha} N_{t-1}^{1-\alpha} + X_{t-1}) \right),$$
(48)

$$W_t = \omega_0 \left(\begin{array}{c} \omega_1 \left((\pi_{y,t} + (1 - \pi_{y,t})(1 - \delta_x)\lambda_{x,t})\alpha_0 k_t^{\alpha} - R_t k_t \right) \\ + (1 - \omega_1) \left(\left(\underline{\pi}_y + (1 - \underline{\pi}_y)(1 - \delta_x)\lambda_x \right) \alpha_0 \underline{k}^{\alpha} - \underline{R} \ \underline{k} \right) \end{array} \right).$$
(49)

D A price-dependent goods-market friction

In the model described in the main text, aggregate supply, $Y_t + X_{t-1}$, is reduced with the fraction $\pi_{y,t}$, and the remaining supply is sold in a competitive market. Free entry implies that the expected profit level associated with job creation is equal to zero. The matching friction, however, implies that existing firm have a positive surplus. Consequently, the question arises whether firms could not affect the goods-market friction they face by changing the price they charge. This appendix develops a version of the model in which firms can affect the amount sold—and thus inventory accumulation—

by changing the price of their products. It is shown that the set of equations characterising the solution to this version of the model is identical to the set of equations given in the main text characterizing the competitive version when the specification of the goods-market friction $\pi_{y,t}$ is slightly adjusted. The intuition underlying this result is that firms do not want to fully "undo" the goods-market friction by lowering their price level, since this benefit of price reduction has to be balanced against the negative impact on firm revenues.

D.1 Specification of the friction

In this version of the model, there is a continuum of firms. If there are no goods-market frictions, then goods sell at the competitive-equilibrium price, $\hat{P}_{\text{CE},t}$, which satisfies the following condition:⁴²

$$\left. \widehat{P}_{\mathrm{CE},t} \left. \frac{\partial U\left(C_{e,t}\right)}{\partial C_{e,t}} \right|_{C_{e,t}=Y_e} = \left(Y_t + X_{t-1}\right)^{-\nu}.$$
(50)

Let $\tilde{\pi}_{iy,t}$ stand for the fraction of goods sold by firm *i*. This fraction consists of a firm specific component, $\tilde{\pi}_{i,t}$, and a common component, $\tilde{\pi}_{y,t}$. In particular,

$$\widetilde{\pi}_{iy,t} = \widetilde{\pi}_{i,t} \widetilde{\pi}_{y,t}.$$
(51)

The firm takes $\tilde{\pi}_{y,t}$ as given, but the firm can affect the *total* goods-market friction it faces, $\tilde{\pi}_{iy,t}$, by changing its price level, $\hat{P}_{i,t}$. The motivation is the following. There are several reasons why a firm may not sell all goods. One possibly reason is that a firm produces goods that customers are not keen to buy. But one would think that reluctant consumers can be persuaded when they can buy the good at a lower price. In particular, $\pi_{i,t}$ is assumed to depend negatively on $\hat{P}_{i,t}/\hat{P}_t$. Thus, the goods-market friction generates a price dependence that is similar to monopolistic competition. More specifically, the firm-specific component is given by⁴³

$$\widetilde{\pi}_{i,t} = \widetilde{\pi}_i \left(\frac{\widehat{P}_{i,t}}{\widehat{P}_t}; \frac{\widehat{P}_t}{\widehat{P}_{\text{CE},t}} \right)$$
(52)

$$\widetilde{\pi}'\left(\frac{\widehat{P}_{i,t}}{\widehat{P}_{t}};\frac{\widehat{P}_{t}}{\widehat{P}_{\text{CE},t}}\right) = \begin{cases} \partial \widetilde{\pi}_{i}\left(\frac{\widehat{P}_{i,t}}{\widehat{P}_{t}};\frac{\widehat{P}_{t}}{\widehat{P}_{\text{CE},t}}\right) / \partial \left(\frac{\widehat{P}_{i,t}}{\widehat{P}_{t}}\right) < 0 & \text{if } \widehat{P}_{t} > \widehat{P}_{\text{CE},t} \\ \partial \widetilde{\pi}_{i}\left(\frac{\widehat{P}_{i,t}}{\widehat{P}_{t}};\frac{\widehat{P}_{t}}{\widehat{P}_{\text{CE},t}}\right) / \partial \left(\frac{\widehat{P}_{i,t}}{\widehat{P}_{t}}\right) < 0 & \text{if } \widehat{P}_{t} = \widehat{P}_{\text{CE},t} \end{cases}$$
(53)

⁴²This is the first-order condition of the household with the consumption levels of the two goods set equal to the supplied quantities.

⁴³If firms have no monopolistic power when $\hat{P}_t = \hat{P}_{CE,t}$, but

The degree of "monopolistic power" is assumed to be smaller if the market price, \hat{P}_t , is closer to the competitive-equilibrium price, $\hat{P}_{\text{CE},t}$. That is,

$$\frac{\partial \left(\partial \widetilde{\pi}_{i}\left(\frac{\widehat{P}_{i,t}}{\widehat{P}_{t}};\frac{\widehat{P}_{t}}{\widehat{P}_{CE,t}}\right)/\partial \left(\widehat{P}_{i,t}/\widehat{P}_{t}\right)\right)}{\partial \left(\frac{\widehat{P}_{t}}{\widehat{P}_{CE,t}}\right)} \begin{cases} < 0 & \text{if } \widehat{P}_{t} > \widehat{P}_{CE,t} \\ \le 0 & \text{if } \widehat{P}_{t} = \widehat{P}_{CE,t} \end{cases}$$
(54)

It is also assumed that

$$\partial \tilde{\pi}_i \left(1; \frac{\hat{P}_t}{\hat{P}_{\text{CE},t}} \right) / \partial \left(\frac{\hat{P}_t}{\hat{P}_{\text{CE},t}} \right) \le 0.$$
(55)

This condition ensures that the goods-market friction does not diminish when the price of the market good increases, at least not in equilibrium when all firms charge the same price.

D.2 Firm problem

The firm problem is now given by

$$\widehat{\boldsymbol{v}}(x_{t-1}; \boldsymbol{S}_t) = \max_{y_t, k_t, x_t, \widehat{P}_{i,t}} \left(\begin{array}{c} \left(\widetilde{\pi}_{iy,t} \left(y_t + x_{t-1} \right) \widehat{P}_{i,t} - \widehat{R}_t k_t - \widehat{W}_t \right) \\ + \beta \left(1 - \delta_n \right) \operatorname{E}_t \left[\Omega_{t+1} \widehat{\boldsymbol{v}}(x_t; \boldsymbol{S}_{t+1}) \right] \end{array} \right)$$
s.t.

$$y_t = \alpha_0 \exp\left(Z_t\right) k_t^{\alpha},\tag{56}$$

$$x_{t} = (1 - \delta_{x}) (1 - \tilde{\pi}_{iy,t}) (y_{t} + x_{t-1}),$$
(57)

$$\widetilde{\pi}_{iy,t} = \widetilde{\pi}_i \left(\frac{\widehat{P}_{i,t}}{\widehat{P}_t}; \frac{\widehat{P}_t}{\widehat{P}_{\text{CE},t}} \right) \widetilde{\pi}_{y,t}.$$
(58)

With firms setting prices, there is an additional first-order condition given by

$$\widetilde{\pi}_{i}\left(\frac{\widehat{P}_{i,t}}{\widehat{P}_{t}};\frac{\widehat{P}_{t}}{\widehat{P}_{\mathrm{CE},t}}\right)\widetilde{\pi}_{y,t} + \widetilde{\pi}_{i}'\left(\frac{\widehat{P}_{i,t}}{\widehat{P}_{t}};\frac{\widehat{P}_{t}}{\widehat{P}_{\mathrm{CE},t}}\right)\widetilde{\pi}_{y,t}\left(\frac{\widehat{P}_{i,t} - (1 - \delta_{x})\,\widehat{\lambda}_{t}}{\widehat{P}_{t}}\right) = 0,\tag{59}$$

where $\hat{\lambda}_t \left(=\lambda_t \hat{P}_t\right)$ is the value of leaving this period with one unit of the good in inventories (after depreciation).

D.3 Equilibrium price level

In equilibrium, $\hat{P}_{i,t} = \hat{P}_t$. Equation (59) then determines the equilibrium price level, \hat{P}_t . That is,

$$\widetilde{\pi}_{i}\left(1;\frac{\widehat{P}_{t}}{\widehat{P}_{\mathrm{CE},t}}\right)\widetilde{\pi}_{y,t}+\widetilde{\pi}_{i}'\left(1;\frac{\widehat{P}_{t}}{\widehat{P}_{\mathrm{CE},t}}\right)\widetilde{\pi}_{y,t}\left(1-\left(1-\delta_{x}\right)\lambda_{t}\right)=0.$$
(60)

The solution does not depend on $\tilde{\pi}_{y,t}$, since the last equation can be rewritten as

$$\widetilde{\pi}_{i}\left(1;\frac{\widehat{P}_{t}}{\widehat{P}_{CE,t}}\right) + \widetilde{\pi}_{i}'\left(1;\frac{\widehat{P}_{t}}{\widehat{P}_{CE,t}}\right)\left(1 - (1 - \delta_{x})\lambda_{t}\right) = 0.$$
(61)

The value of $\tilde{\pi}_{y,t}$ still affects firm profits and, thus, employment, but it does not affect prices.

Equation (61) solves for $\hat{P}_t/\hat{P}_{CE,t}$ as a function of λ_t . Consequently, $\tilde{\pi}_{i,t}$ is a function of λ_t only. With some abuse of notation, this function is denoted by $\tilde{\pi}_i(\lambda_t)$. The total goods-market friction, $\tilde{\pi}_{iy,t}$, only depends on $\tilde{\pi}_{y,t}$ and λ_t , since

$$\widetilde{\pi}_{iy,t} = \widetilde{\pi}_{i,t} \widetilde{\pi}_{y,t} = \widetilde{\pi}_i \left(1, \frac{\widehat{P}_t}{\widehat{P}_{\text{CE},t}} \right) \widetilde{\pi}_{y,t} = \widetilde{\pi}_i \left(\lambda_t \right) \widetilde{\pi}_{y,t}.$$
(62)

To understand how close this version of the model is to the model developed in the main text, consider the case when $\delta_x = 1.^{44}$ In this case, $\hat{P}_t/\hat{P}_{\text{CE},t}$ and $\tilde{\pi}_{i,t}$ would also be constant. Consequently, the version with a price-dependent goods-market friction would be identical to the model developed in the main text except that $\tilde{\pi}_{y,t}$ is scaled with a constant $\tilde{\pi}_{i,t}$. Since the calibration focuses on the total goods market friction, i.e., $\tilde{\pi}_{iy,t}$, this would not affect the results.

Now consider the general case with $\delta_x < 1$. How do changes in λ_t affect the goods-market friction. It is assumed that the conditions given in equations (54) and (55)are satisfied. Moreover, it is assumed that there is an internal solution to equation (61). That is, $\hat{P}_t > \hat{P}_{\text{CE},t}$. then an increase in λ_t would lead to an increase in $\hat{P}_t/\hat{P}_{\text{CE},t}$ and a decrease in $\tilde{\pi}_{i,t}$. That is, in equilibrium firms prefer to charge a higher price and sell less. This is intuitive, since λ_t is the value the firm gets if it does not sell.

D.4 Comparison with benchmark version

The version of the model developed in this appendix endogenizes firm-level price setting and, thus, inventory accumulation. That is, although firms still face a goods market friction they could choose to (partially) undo its impact by charging lower prices. The fraction sold in period t is equal to

$$\widetilde{\pi}_{iy,t} = \widetilde{\pi}_i \left(\lambda_t \right) \widetilde{\pi}_{y,t}. \tag{63}$$

The value of λ_t , and thus the value of $\tilde{\pi}_{i,t}$, is a function of the state variables, Z_t , K_{t-1} , N_{t-1} , and X_{t-1} . With another abuse of notation, this function is denoted $\tilde{\pi}_i(Z_t, K_{t-1}, N_{t-1}, X_{t-1})$. Thus,

$$\widetilde{\pi}_{iy,t} = \widetilde{\pi}_i \left(Z_t, K_{t-1}, N_{t-1}, X_{t-1} \right) \widetilde{\pi}_{y,t}.$$
(64)

⁴⁴The same conclusion can be drawn if λ_t would be constant, but this condition is not satisfied.

The *iy* subscript indicates that the goods-market efficiency measures comprises both the firm-specific and the common component. Note, however, that $\tilde{\pi}_{iy,t}$ is the same for all firms, since the value of λ_t is the same for all firms.

 $\widetilde{\pi}_i(Z_t, K_{t-1}, N_{t-1}, X_{t-1})$ is a fixed function of the state variables. Suppose that

$$\widetilde{\pi}_{y,t} = \frac{\pi_{y,t}}{\widetilde{\pi}_i \left(Z_t, K_{t-1}, N_{t-1}, X_{t-1} \right)},\tag{65}$$

where $\pi_{y,t}$ is the specification of the goods-market friction in the benchmark version of the model. In this case,

$$\widetilde{\pi}_{iy,t} = \widetilde{\pi}_i \left(\lambda_t \right) \widetilde{\pi}_{y,t} = \pi_{y,t}.$$
(66)

For this specification of $\tilde{\pi}_{y,t}$, the friction that firms face in the economy with a price-dependent goods-market friction, $\tilde{\pi}_{iy,t}$, is exactly equal to the friction that firms face in the benchmark version of the model, $\pi_{y,t}$. That is, the model with a price-dependent goods-market friction is identical to the benchmark version of the model when $\pi_{y,t}$ is modified as in equation (65). Moreover, if the behavior of $\pi_{y,t}$ is consistent with properties of its empirical counterpart, then the same is true for the behavior of $\tilde{\pi}_{iy,t}$. As documented in appendix D.5, the modification of $\pi_{y,t}$ is relatively minor.

Now suppose that $\tilde{\pi}_{y,t} = \pi_{y,t}$. In this case, the behavior of the friction that firms face is different in the two economies. The question arises whether fluctuations in the firm-specific component, $\tilde{\pi}_i(\lambda_t)$, dampen or amplify fluctuations in $\tilde{\pi}_{y,t}$. Recall that λ_t denotes the value of leaving period twith a unit of the good in inventories and that $\tilde{\pi}_i(\lambda_t)$ depends negatively on λ_t . Inventory accumulation is a form of savings and the value of savings increases if agents become richer. Consequently, $\tilde{\pi}_i(\lambda_t)$ depends negatively on Z_t , K_{t-1} , and N_{t-1} , whereas $\tilde{\pi}_{y,t} (= \pi_{y,t})$ depends positively on these three variables. This means that firms would adjust prices to partly offset changes in $\tilde{\pi}_{y,t}$. This means that $\tilde{\pi}_{y,t}$ would have to be more cyclical than $\pi_{y,t}$, if $\tilde{\pi}_{iy,t}$ is equal to $\pi_{y,t}$.

Now consider the effect of X_{t-1} on $\tilde{\pi}_i(\lambda_t)$. Starting the period with a larger stock of goods mean that the agent is richer, which in turn implies that $\tilde{\pi}_i(\lambda_t)$ depends negatively on X_{t-1} .⁴⁵ Thus, the ability of firms to affect the goods-market friction actually amplifies the dependence of the goodsmarket friction on aggregate inventories. Note $\tilde{\pi}_{iy,t}$ also depends negatively on aggregate inventories when $\tilde{\pi}_{y,t}$ does not depend on X_{t-1} , that is when $\zeta_x = 0$. Endogenous price setting can, thus, explain the observed negative dependence of the goods-market friction on aggregate inventories.

⁴⁵If an increase in X_{t-1} has a very large negative impact on $\tilde{\pi}_{y,t}$, then an increase in inventories could reduce welfare and a social planner would like to destory inventories. But this possibility is not plausible.

D.5 Example to document similarity

The firm-specific component of the goods-market friction is given by

$$\widetilde{\pi}_{i,t} = \Gamma_0 - \Gamma_{1,t} \times \frac{\widehat{P}_{i,t}}{\widehat{P}_t} \text{ with}$$
(67)

$$\Gamma_{1,t} = \Gamma_1 \left(\frac{\widehat{P}_t}{\widehat{P}_{CE,t}} \right)$$
 and (68)

$$\frac{\partial \Gamma_1(x)}{\partial x} < 0. \tag{69}$$

That is, a firm can lower the goods-market friction it faces by lowering its price level, $\hat{P}_{i,t}$. The extent to which the firm can do so is given by $\Gamma_{1,t}$. The closer the price level is to the competitive equilibrium outcome, the lower the value of $\Gamma_{1,t}$, that is, the harder it is for firms to affect the goods-market friction.

For this specification of $\tilde{\pi}_{i,t}$, equation (61) can be written as

$$\Gamma_0 - \Gamma_{1,t} - \Gamma_{1,t} \left(1 - (1 - \delta_x) \lambda_{x,t} \right) = 0, \tag{70}$$

which implies that

$$\Gamma_{1,t} = \frac{\Gamma_0}{2 - (1 - \delta_x) \lambda_{x,t}} \tag{71}$$

and

$$\widetilde{\pi}_{i,t} = \Gamma_0 \left(\frac{1 - (1 - \delta_x) \lambda_{x,t}}{2 - (1 - \delta_x) \lambda_{x,t}} \right).$$
(72)

The value of Γ_0 is chosen to ensure that $\tilde{\pi}_{i,t}$ is equal to 1 in steady state.

Figure 7 plots $\pi_{y,t}$ using the calibration from the main text when all inventory facts are matched for the indicated value of ρ . Thus, $\zeta_x < 0$. It also plots $\pi_{y,t}/\tilde{\pi}_{i,t}$. This is the specification for $\tilde{\pi}_{y,t}$ such that the total goods-market friction in the model with a price-dependent friction is identical to the friction of the benchmark version of the model.⁴⁶ The graph shows that the behavior is fairly similar. Consistent with the discussion above, $\pi_{y,t}/\tilde{\pi}_i (Z_t, K_{t-1}, N_{t-1}, X_{t-1})$ is more volatile than $\pi_{y,t}$. That is, to end up with the same cyclical behavior for the total goods-market efficiency measure in the model with a price-dependent goods-market friction, one needs a somewhat stronger market-size externality.

⁴⁶For both values of ρ , the steady state value of $\Gamma_{1,t}$ is equal to 0.76. That is, if a firm lowers its price level, $\hat{P}_{i,t}$, to a level that is 1% below the average price level, \hat{P}_t , then the goods market friction this firm faces decreases with 0.76%.

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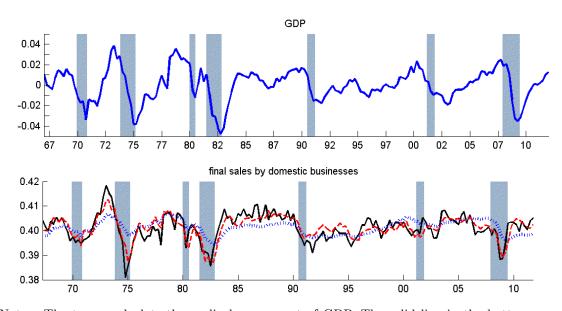


Figure 1: Cyclical behavior of goods-market efficiency

Notes: The top panel plots the cyclical component of GDP. The solid line in the bottom panel is the cyclical component of goods-market efficiency (plus the mean). If the efficiency measure is equal to 0.5, then sales are 50% of newly produced output plus inventories. The bottom panel also plots the fitted values from a projection using cyclical GDP (dotted line) and the fitted values from a projection using cyclical inventories (dashed line).

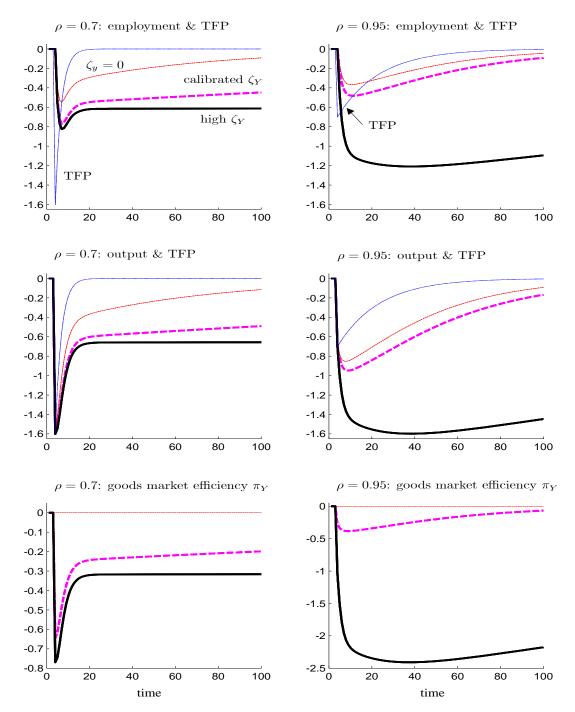


Figure 2: IRFs when not all key inventory facts are matched

Notes: Each panel plots the responses to a productivity shock. The IRF labeled "calibrated ζ_y " corresponds to the case when ζ_y and ω_0 are chosen to match σ_N/σ_Y and σ_{π_y}/σ_Y . This version of the model does not match the observed value of σ_S/σ_Y .

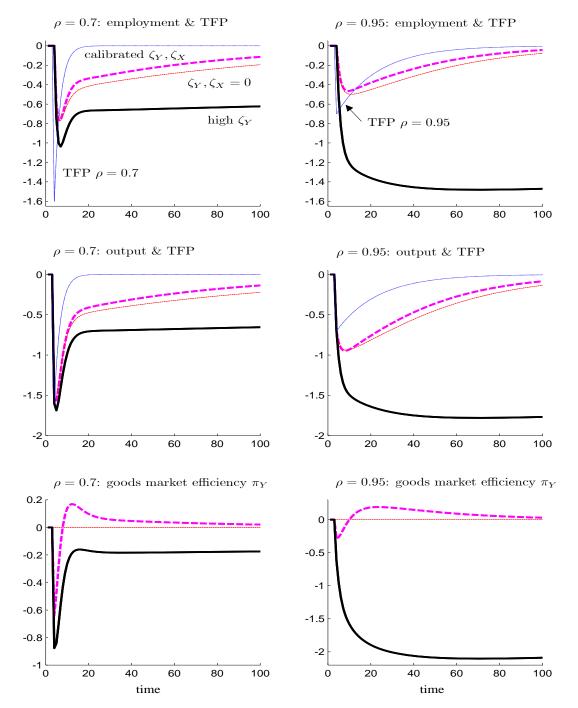


Figure 3: IRFs when key inventory facts are matched

Notes: Each panel plots the responses to a productivity shock. The IRF labeled "calibrated ζ_y, ζ_x " corresponds to the case when ζ_y, ζ_x , and ω_0 are chosen to match $\sigma_N/\sigma_Y, \sigma_{\pi_y}/\sigma_Y$, and σ_S/σ_Y .

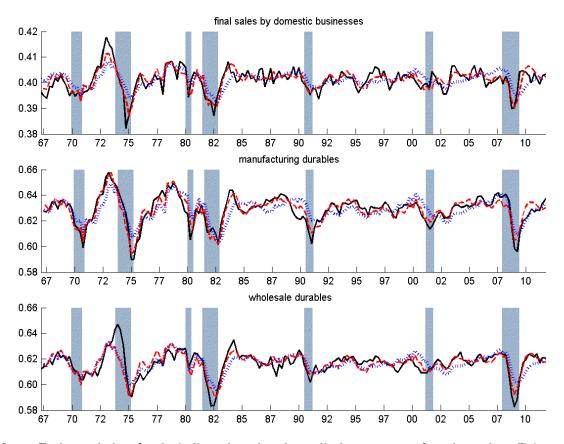


Figure 4: Fitted goods-market efficiency (detrending with the HP filter)

Notes: Each panel plots for the indicated market the cyclical component of goods-market efficiency (solid line), the fitted values from a regression using cyclical GDP (dotted line), and the fitted values from a regression using cyclical GDP and lagged cyclical inventories (dashed line). If the efficiency measure is equal to 0.5, then sales are 50% of newly produced output plus inventories.

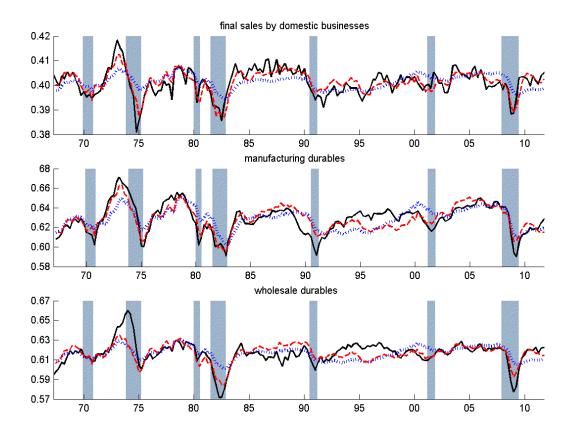


Figure 5: Fitted goods-market efficiency (detrending with a deterministic trend)

Notes: Each panel plots for the indicated market the cyclical component of goods-market efficiency (solid line), the fitted values from a regression using cyclical GDP (dotted line), and the fitted values from a regression using cyclical GDP and lagged cyclical inventories (dashed line). If the efficiency measure is equal to 0.5, then sales are 50% of newly produced output plus inventories.

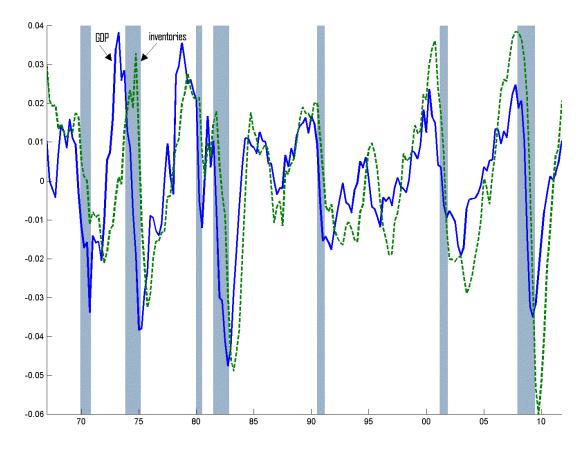


Figure 6: Cyclical behavior of GDP and non-farm inventories

Notes: Data are detrended using the HP filter.

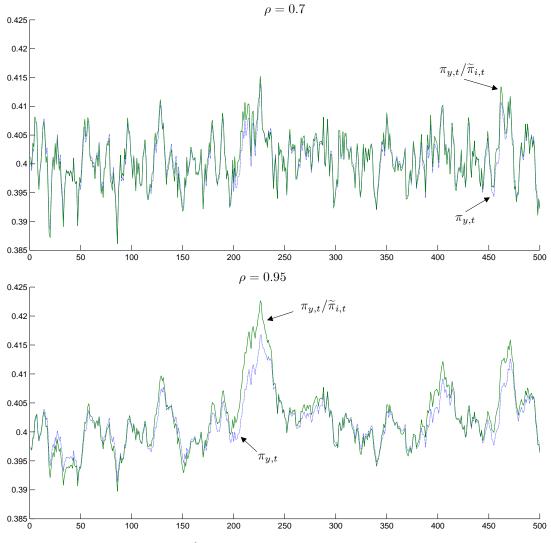


Figure 7: Modification of $\pi_{y,t}$ needed to get identical results in both versions

Notes: The panels plot timeseries for $\pi_{y,t}$ generated by the benchmark version when all inventory facts are matched. It also plots the value of $\tilde{\pi}_{y,t}$ such that the version of the model with a price-dependent goods-market friction is identical to the benchmark version, i.e., $\pi_{y,t}/\tilde{\pi}_i(\lambda_{x,t})$.

	total	goods + structures
$ \begin{array}{c} \rho_{X,S} \\ \rho_{X,S}, BP_{\leq 4Q} \\ \rho_{X,S}, BP_{\leq 8Q} \\ \rho_{\Delta X,S} \end{array} $	0.632 -0.364 -0.269 0.356	0.648 -0.358 -0.270 0.361
$\sigma_S / \sigma_Y \\ \rho_{X,S}, BP_{\leq 4Q} \\ \rho_{X,S}, BP_{\leq 8Q}$	$0.909 \\ 1.033 \\ 1.006$	$0.902 \\ 0.970 \\ 0.972$
$ \begin{array}{l} \mathrm{mean} \ \pi_{y,t} \\ \mathrm{mean} \ X_t/S_t \end{array} $	$0.550 \\ 0.821$	$0.401 \\ 1.498$
$\sigma_{\pi_y} \sigma_{\pi_y} / \sigma_S$	$0.0041 \\ 0.215$	$0.0047 \\ 0.184$
$\rho_{\pi_y,Y}\\\rho_{\pi_y,X_{-1}}$	0.362 -0.508	0.607 -0.251

Table 1: Summary statistics - Private non-farm inventories and final sales

Notes: $BP_{\leq NQ}$ indicates that the band-pass filter is used to extract that part of the series that is associcated with fluctuations with a period less than N quarters. All other secondorder moments are for HP-detrended data. σ_i is the standard deviation of variable i; $\rho_{i,j}$ is the correlation coefficient of variables i and j; S stands for sales, X stands for inventories, Y stands for GDP, and $\pi_y = S/(Y + X_{-1})$ is the measure of goods-market efficiency.

	data	model with $ ho=0.7$			model with $\rho = 0.95$			
		$\begin{array}{c} \zeta_y, \omega_0 \\ \text{calibrated} \end{array}$	$\zeta_y=0$	high ζ_Y	$\begin{array}{c} \zeta_y, \omega_0 \\ \text{calibrated} \end{array}$	$\zeta_y=0$	high ζ_y	
	parameter values							
ζ_y		0.162	0	0.193	0.162	0	0.600	
ζ_x		0	0	0	0	0	0	
ω_0		0.993	0.993	0.993	0.970	0.970	0.970	
			ca	alibrated mor	nents			
σ_N/σ_Y	0.466	=	0.357	0.499	=	0.386	0.732	
σ_{π_Y}/σ_Y	0.162	=	0	0.189	=	0	0.566	
σ_S/σ_Y	0.901	1.006	0.775	1.064	1.045	0.853	1.823	
			in	ventory prop	perties			
$\rho_{X,S}$	0.648	0.674	0.845	0.644	0.803	0.913	-0.509	
$\rho_{X,S}, BP_{\leq 4Q}$	-0.358	-0.690	-0.485	-0.700	-0.602	-0.364	0.485	
$\rho_{X,S}, BP_{\leq 8Q}$	-0.270	-0.086	0.286	-0.118	0.010	0.369	0.123	
		standard business cycle statistics						
σ_C/σ_Y	0.535	0.338	0.238	0.367	0.447	0.354	0.896	
σ_I / σ_Y	3.554	3.710	2.906	3.935	3.199	2.676	12.431	
		role of i	nvestment i	in inventorie	s for GDP flue	etuations		
ρ_{XY}/σ_Y^2	0.193	0.149	0.384	0.108	0.094	0.316	-0.461	
			autocorr	relation unfil	tered series			
$\rho_{N,N(-1)}$		0.982	0.9153	0.994 $^{'}$	0.993	0.989	0.999	
$\rho_{Y,Y(-1)}$		0.997	0.984	0.999	0.996	0.995	1.000	

Table 2: Results when not all key inventory facts are matched

Notes: This table reports summary statistics of model-generated data and the empirical counterparts. $BP_{\leq NQ}$ indicates that the band-pass filter is used to extract that part of the series that is associated with fluctuations with a period less than N quarters. All other second-order moments are for HP-detrended data. σ_i is the standard deviation of variable i; $\rho_{i,j}$ is the correlation coefficient of variables i and j; S stands for sales, X stands for inventories, Y stands for GDP, Y^* is the output measure for these firms data (constructed using the sales and inventory data), and $\pi_y = S/(Y + X_{-1})$ is the measure of goods-market efficiency. ρ is the autoregressive coefficient in the law of motion for productivity, Z_t . For both values of ρ , the table has three columns. The first column gives the results when ζ_y and ω_0 are chosen to match σ_N/σ_Y and σ_{π_y}/σ_Y . Not matched is the value of σ_S/σ_Y . The second column gives the results when ζ_y is set equal to 0. The third column gives the results when ζ_y is set to the highest possible value for which model data are non-explosive. "=" indicates that this model characteristic matches its empirical counterpart by construction.

	data	ma	odel $\rho = 0.7$		mo	$del \ \rho = 0.9$	5		
		$\zeta_y, \zeta_x, \omega_0$ calibrated	$\begin{array}{l} \zeta_y = 0 \\ \zeta_x = 0 \end{array}$	high ζ_y	$\begin{array}{c} \zeta_y, \zeta_x, \omega_0 \\ \text{calibrated} \end{array}$	$\begin{array}{l} \zeta_y = 0 \\ \zeta_x = 0 \end{array}$	high ζ_y		
parameter values									
Ċ		0.161	0	0.220	0.161	0	0.355		
$\zeta_y \ \zeta_x$		-0.178	0	-0.178	-0.191	0	-0.191		
ω_0		0.993	0.993	0.993	0.980	0.980	0.980		
		calibrated moments							
σ_N/σ_Y	0.466	=	0.474	0.582	=	0.488	0.757		
σ_{π_y}/σ_Y	0.162	=	0	0.211	=	0	0.314		
σ_S / σ_Y	0.901	=	0.788	1.046	=	0.861	2.521		
			in^{*}	ventory prop	perties				
$\rho_{X,S}$	0.648	0.327	0.858	0.326	0.433	0.919	-0.228		
$\rho_{X,S}, BP_{\leq 4Q}$	-0.358	-0.741	-0.456	-0.721	-0.519	-0.323	0.128		
$\rho_{X,S}, BP_{\leq 8Q}$	-0.270	-0.362	0.903	-0.351	-0.215	0.340	0.050		
		standard business cycle statistics							
σ_C/σ_Y	0.535	0.252	0.262	0.353	0.359	0.378	1.008		
σ_I/σ_Y	3.554	3.571	2.910	3.92	2.903	2.724	16.900		
	role of investment in inventories for GDP fluctuations								
ρ_{XY}/σ_Y^2	0.193	0.240	0.372	0.118	0.259	0.308	-0.265		
	autocorrelation unfiltered series								
$\rho_{N,N(-1)}$		0.933	0.949	0.991	0.990	0.992	1.000		
$\rho_{Y,Y(-1)}$		0.977	0.987	0.998	0.993	0.995	1.000		

Table 3: Results when all key inventory facts are matched

Notes: This table reports summary statistics of model-generated data and the empirical counterparts. $BP_{\leq NQ}$ indicates that the band-pass filter is used to extract that part of the series that is associated with fluctuations with a period less than N quarters. All other second-order moments are for HP-detrended data. σ_i is the standard deviation of variable i; $\rho_{i,j}$ is the correlation coefficient of variables i and j; S stands for sales, X stands for inventories, Y stands for GDP, Y^* is the output measure for these firms data (constructed using the sales and inventory data), and $\pi_y = S/(Y + X_{-1})$ is the measure of goods-market efficiency. ρ is the autoregressive coefficient in the law of motion for productivity, Z_t . For both values of ρ , the table has three columns. The first column gives the results when ζ_y , ζ_x , and ω_0 are chosen to match σ_N/σ_Y , σ_S/σ_Y , and σ_{π_y}/σ_Y . The second column gives the results when ζ_y and ζ_x are set equal to 0. The third column gives the results when ζ_y is set to the highest possible value for which model data are non-explosive. "="

	manufacturing		wł	retail	
	durable	non-durable	durable	non-durable	
$\rho_{X,S}$	0.416	0.338	0.646	0.434	0.687
$\rho_{X,S}, BP_{\leq 4Q}$	0.079	-0.104	-0.004	0.056	-0.159
$\rho_{X,S}, BP_{\leq 8Q}$	-0.121	0.078	0.098	0.262	-0.167
$\rho_{\Delta X,S}$	0.626	0.330	0.449	0.049	0.231
σ_S/σ_Y	0.973	0.977	0.964	0.985	0.943
$\rho_{X,S}, BP_{\leq 4Q}$	0.972	0.945	0.781	0.902	0.922
$\rho_{X,S}, BP_{\leq 8Q}$	0.978	0.931	0.890	0.936	0.962
mean π_y	0.628	0.732	0.616	0.786	0.683
mean X/S	0.594	0.367	0.630	0.274	0.465
σ	0.0113	0.0049	0.0096	0.0043	0.0043
$\sigma_{\pi_y} \sigma_{\pi_y} / \sigma_S$	0.22	0.19	0.18	0.18	0.17
ρ_{π_y,Y^*}	0.812	0.744	0.759	0.331	0.323
$\rho_{\pi_y,Y}$	0.753	0.524	0.718	0.085	0.058
$\rho_{\pi_y,X_{-1}}$	-0.373	-0.402	-0.145	-0.390	-0.356

Table 4: Summary statistics - Sectoral inventory and gross sales data

Notes: $BP_{\leq NQ}$ indicates that the band-pass filter is used to extract that part of the series that is associcated with fluctuations with a period less than N quarters. All other second-order moments are for HP-detrended data. σ_i is the standard deviation of variable i; $\rho_{i,j}$ is the correlation coefficient of variables i and j; S stands for sales, X stands for inventories, Y stands for GDP, Y^* is the output measure for the group of firms considered (constructed using the sales and inventory data), and $\pi_y = S/(Y + X_{-1})$ is the measure of goods-market efficiency.

	$\widetilde{\pi}_{y,t} = \zeta_y \widetilde{Y}_t + \zeta_x \widetilde{X}_{t-1}$		$\widetilde{\pi}_{y,t} = \zeta_y \widetilde{Y}_t$	
	ζ_y	ζ_x	R^2	R^2
HP detrending				
final sales	0.25	-0.14	0.67	0.38
gross sales				
dur. manufacturing	0.60	-0.20	0.82	0.57
nondur. manufacturing	0.21	-0.17	0.60	0.27
dur. wholesale	0.51	-0.12	0.66	0.52
nondur. wholesale	0.06	-0.07	0.19	0.006
retail	0.13	-0.11	0.27	0.004
detrending with time trend				
final sales	0.25	-0.13	0.67	0.27
gross sales				
dur. manufacturing	0.52	-0.16	0.72	0.50
nondur. manufacturing	0.16	-0.13	0.50	0.18
dur. wholesale	0.42	-0.11	0.51	0.29
nondur. wholesale	0.18	-0.13	0.57	0.21
retail	0.19	-0.11	0.45	0.00

Table 5: Cyclicality of observed goods-market efficiency

Notes: All series are detrended by the indicated detrending procedure. The last column displays the R^2 when goods-market efficiency, $\tilde{\pi}_{y,t}$, is projected on GDP, \tilde{Y}_t , only. The other three columns display the projection coefficients and the R^2 when $\tilde{\pi}_{y,t}$ is projected on GDP and beginning-of-period t inventories, \tilde{X}_{t-1} .